Parametrization of the planetary boundary layer (PBL)

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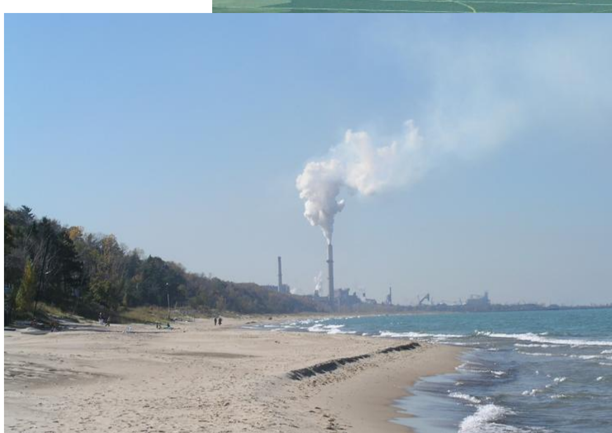
Surface layer and surface fluxes	Irina
Outer layer	Irina
Stratocumulus	Irina
PBL evaluation	*Maike*
Exercises	*Irina & Maike*

Why studying the Planetary Boundary Layer ?

- Natural environment for human activities
- Understanding and predicting its structure
  - Agriculture, aeronautics, telecommunications, Earth energetic budget
- Weather forecast, pollutants dispersion, climate prediction





Outline

- ☞ Definition
- ☞ Turbulence
- ☞ Stability
- ☞ Classification
- ☞ Clear convective boundary layers
- ☞ Cloudy boundary layers (stratocumulus and cumulus)
- ☞ Summary

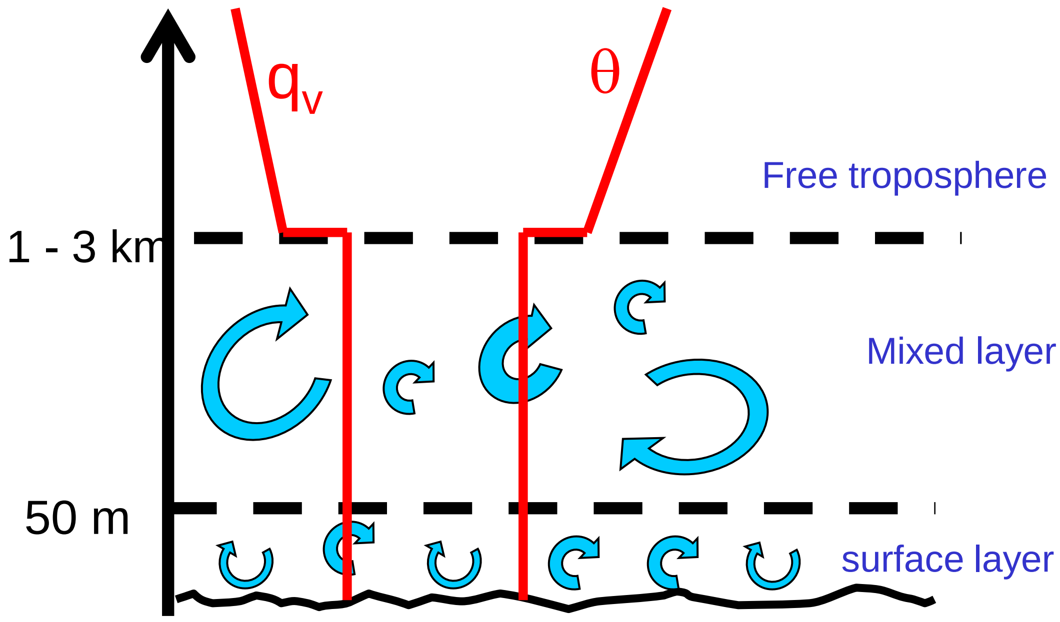
PBL: Definitions

The PBL is the layer close to the surface within which vertical transports by turbulence play dominant roles in the momentum, heat and moisture budgets.

☞ The layer where the flow is turbulent.

☞ The fluxes of momentum, heat or matter are carried by turbulent motions on a scale of the order of the depth of the boundary layer or less.

☞ The surface effects (friction, cooling, heating or moistening) are felt on times scales < 1 day.



Composition

- atmospheric gases (N_2, O_2, water vapor, …)
- aerosol particles
- clouds (condensed water)

PBL: Turbulence

Characteristics of the flow

- Rapid variation in time
- Irregularity
- Randomness

} **Chaotic flow**

Properties

- Diffusive
- Dissipative
- Irregular (butterfly effect)

Origin:

- Hydrodynamic instability (wind shear)

- Thermal instability

PBL: Governing equations for the mean state

- gas law (equation of state)
- momentum (Navier Stokes)
- continuity eq. (conservation of mass)
- heat (first principle of thermodynamics)
- total water

Reynolds averaging $A = \overline{A} + A'$

Averaging (overbar) is over grid box, i.e. sub-grid turbulent motion is averaged out.

Simplifications

Boussinesq approximation (density fluctuations non-negligible only in buoyancy terms)

Hydrostatic approximation (balance of pressure gradient and gravity forces)

Incompressibility approximation (changes in density are negligible)

PBL: Governing equations for the mean state

Reynolds averaging $A = \overline{A} + A'$

gas law $\overline{p} = \overline{\rho}\, R_d\, \overline{T_v}$ $\overline{T_v} = T(1 + 0.61 q_v - q_l)$

virtual temperature

PBL: Governing equations for the mean state

Reynolds averaging $A = \overline{A} + A'$

Need to be parameterized !

☞ gas law $\overline{p} = \overline{\rho} \; R_d \; \overline{T_v}$ $\qquad \overline{T_v} = T(1 + 0.61 q_v - q_l)$

virtual temperature

2nd order

☞ momentum

$$\frac{\partial \overline{u_i}}{\partial t} + \overline{u_j} \frac{\partial \overline{u_i}}{\partial x_j} = -\delta_{i3} g + f_c \varepsilon_{ij3} \overline{u_j} - \frac{1}{\overline{\rho}} \frac{\partial \overline{P}}{\partial x_i} + \frac{\upsilon \partial^2 \overline{u_i}}{\partial x_j{}^2} - \frac{\partial (\overline{u_i' u_j'})}{\partial x_j}$$

mean advection | gravity | Coriolis | Pressure gradient | Viscous stress | Turbulent transport

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mean advection | gravity | Coriolis | Pressure gradient | Viscous stress | Turbulent transport

- continuity eq. $\frac{\partial \overline{u_i}}{\partial x_j} = 0$

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mean advection | gravity | Coriolis | Pressure gradient | Viscous stress | Turbulent transport

- continuity eq. $\frac{\partial \overline{u_i}}{\partial x_j} = 0$

- heat

$$\frac{\partial \overline{\theta}}{\partial t} + \overline{u_j}\frac{\partial \overline{\theta}}{\partial x_j} = -\frac{1}{\overline{\rho} c_p}\frac{\partial \overline{F_j}}{\partial x_j} - \frac{\partial \overline{u_j' \theta'}}{\partial x_j} - \frac{L_v E}{\overline{\rho} c_p}$$

mean advection | radiation | turbulent transport | Latent heat release

PBL: Governing equations for the mean state

Reynolds averaging $A = \overline{A} + A'$

- gas law $\bar{p} = \bar{\rho} R_d \overline{T_v}$ $\overline{T_v} = T(1 + 0.61 q_v - q_l)$

virtual temperature

2nd order

- momentum

$$\frac{\partial \overline{u_i}}{\partial t} + \overline{u_j}\frac{\partial \overline{u_i}}{\partial x_j} = -\delta_{i3} g + f_c \varepsilon_{ij3} \overline{u_j} - \frac{1}{\overline{\rho}}\frac{\partial \overline{P}}{\partial x_i} + \frac{\upsilon \partial^2 \overline{u_i}}{\partial x_j{}^2} - \frac{\partial (\overline{u_i' u_j'})}{\partial x_j}$$

mean advection | gravity | Coriolis | Pressure gradient | Viscous stress | Turbulent transport

- continuity eq.

$$\frac{\partial \overline{u_i}}{\partial x_j} = 0$$

- heat

$$\frac{\partial \overline{\theta}}{\partial t} + \overline{u_j}\frac{\partial \overline{\theta}}{\partial x_j} = -\frac{1}{\overline{\rho} c_p}\frac{\partial \overline{F_j}}{\partial x_j} - \frac{\partial \overline{u_j' \theta'}}{\partial x_j} - \frac{L_v E}{\overline{\rho} c_p}$$

mean advection | radiation | turbulent transport | Latent heat release

- total water

$$\frac{\partial \overline{q_t}}{\partial t} + \overline{u_j}\frac{\partial \overline{q_t}}{\partial x_j} = \frac{S_{q_t}}{\overline{\rho}} - \frac{\partial \overline{u_j' q_t'}}{\partial x_j}$$

mean advection | precipitation | turbulent transport

PBL: Turbulent kinetic energy equation

☞ TKE: a measure of the intensity of turbulent mixing $\bar{e} = \frac{1}{2}(\overline{u'^2} + \overline{v'^2} + \overline{w'^2})$

$$\frac{\partial \bar{e}}{\partial t} + \overline{u}_j \frac{\partial \bar{e}}{\partial x_j} = \frac{g}{\theta_0}\overline{w'\theta_v'} - \overline{u_i' u_j'}\frac{\partial \overline{u_i}}{\partial x_j} - \frac{\partial \overline{u_j' e}}{\partial x_j} - \frac{1}{\rho}\frac{\partial \overline{u_i' p'}}{\partial x_i} - \varepsilon$$

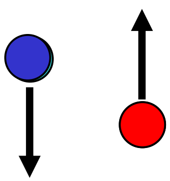
buoyancy production | mechanical shear | turbulent transport | pressure transport | dissipation

$$\theta_v = \theta\left(1 + 0.61 q_v - q_l\right)$$

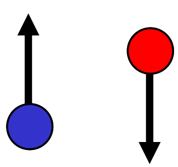
virtual potential temperature

☞ An example :

✘ $\theta_v' < 0$, $w' < 0$ or $\theta_v' > 0$, $w' > 0$ ⟶ $w' \theta_v' > 0$ source



✘ $\theta_v' < 0$, $w' > 0$ or $\theta_v' > 0$, $w' < 0$ ⟶ $w' \theta_v' < 0$ sink

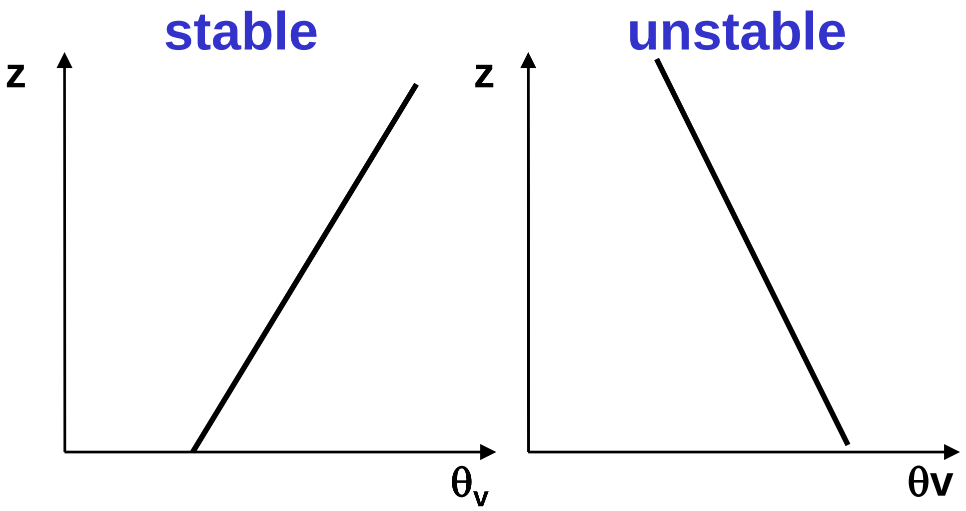


PBL: Stability (I)

☞ Traditionally stability is defined using the temperature gradient

☞ θ_v gradient (local definition):

- $\frac{\partial \overline{\theta_v}}{\partial z} > 0$ stable layer
- $\frac{\partial \overline{\theta_v}}{\partial z} < 0$ unstable layer
- $\frac{\partial \overline{\theta_v}}{\partial z} = 0$ neutral layer

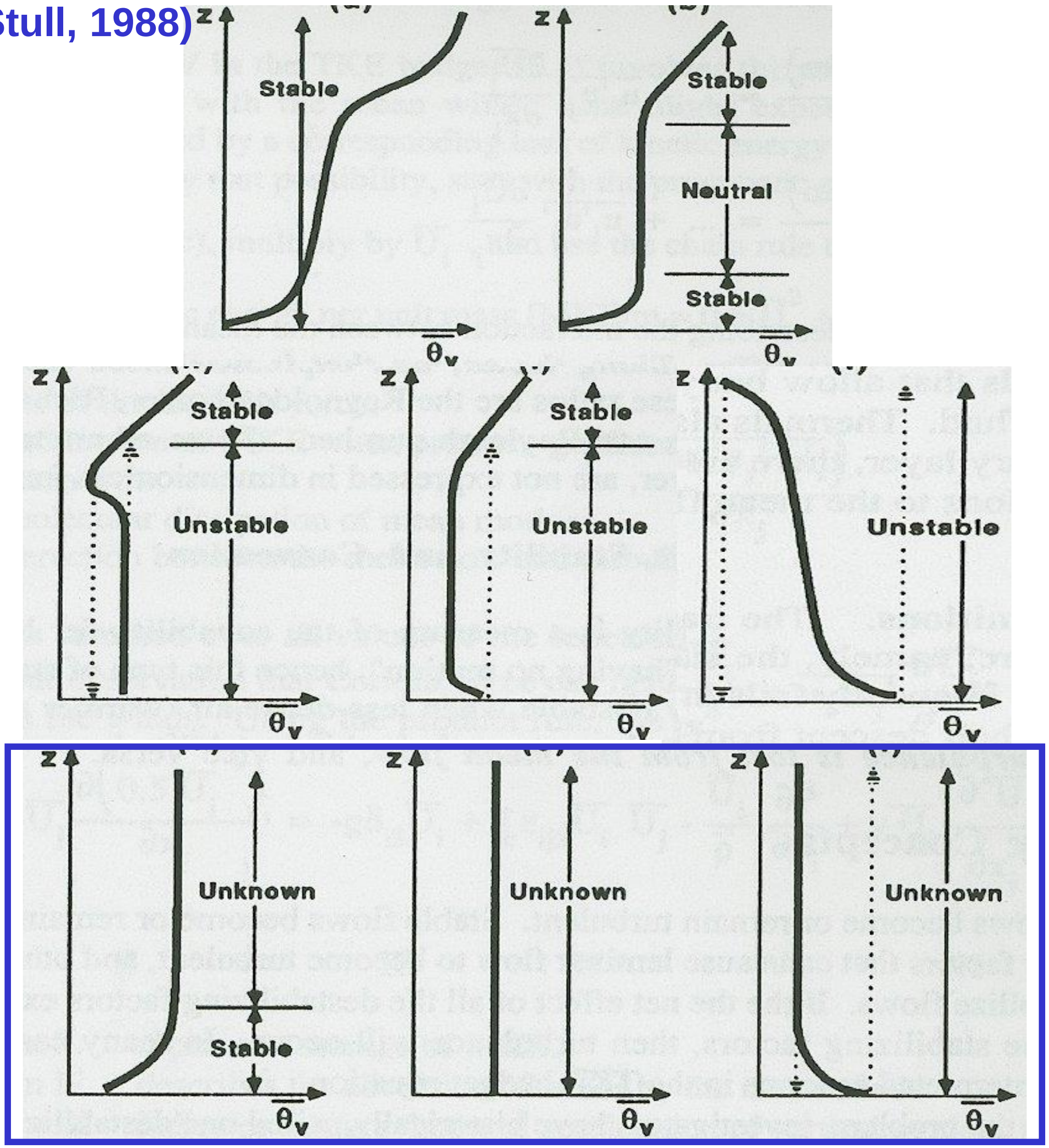


☞ How to determine the stability of the PBL taken as a whole ?

- In a mixed layer the gradient of temperature is practically zero
- Either θ_v or w' θ_v' profiles are needed to determine the PBL stability state

PBL: Stability (II)

(Stull, 1988)



Stable

Unstable

?

PBL: Other ways to determine stability (III)

Bouyancy flux at the surface:

$\overline{w'\theta_v'} > 0$ unstable PBL (convective)

$\overline{w'\theta_v'} < 0$ stable PBL

$\overline{w'\theta_v'} = 0$ neutral PBL

Or dynamic production of TKE integrated over the PBL depth stronger than thermal production

Monin-Obukhov length:

$$L = \frac{-\overline{\theta}_v u_*^3}{kg(\overline{w'\theta_v'})_s}, \quad u_*^2 = (\overline{u'w'})_s$$

$-10^5\text{m} \le L \le -100\text{m}$	unstable PBL
$-100\text{m} < L < 0$	strongly unstable PBL
$0 < L < 10$	strongly stable PBL
$10\text{m} \le L \le 10^5\text{m}$	stable PBL
$\|L\| > 10^5\text{m}$	neutral PBL

PBL: Classification and scaling

☞ Neutral PBL :

- turbulence scale l ~ 0.07 H, H being the PBL depth
- Quasi-isotropic turbulence
- Scaling - adimensional parameters : z_0, H, u_*

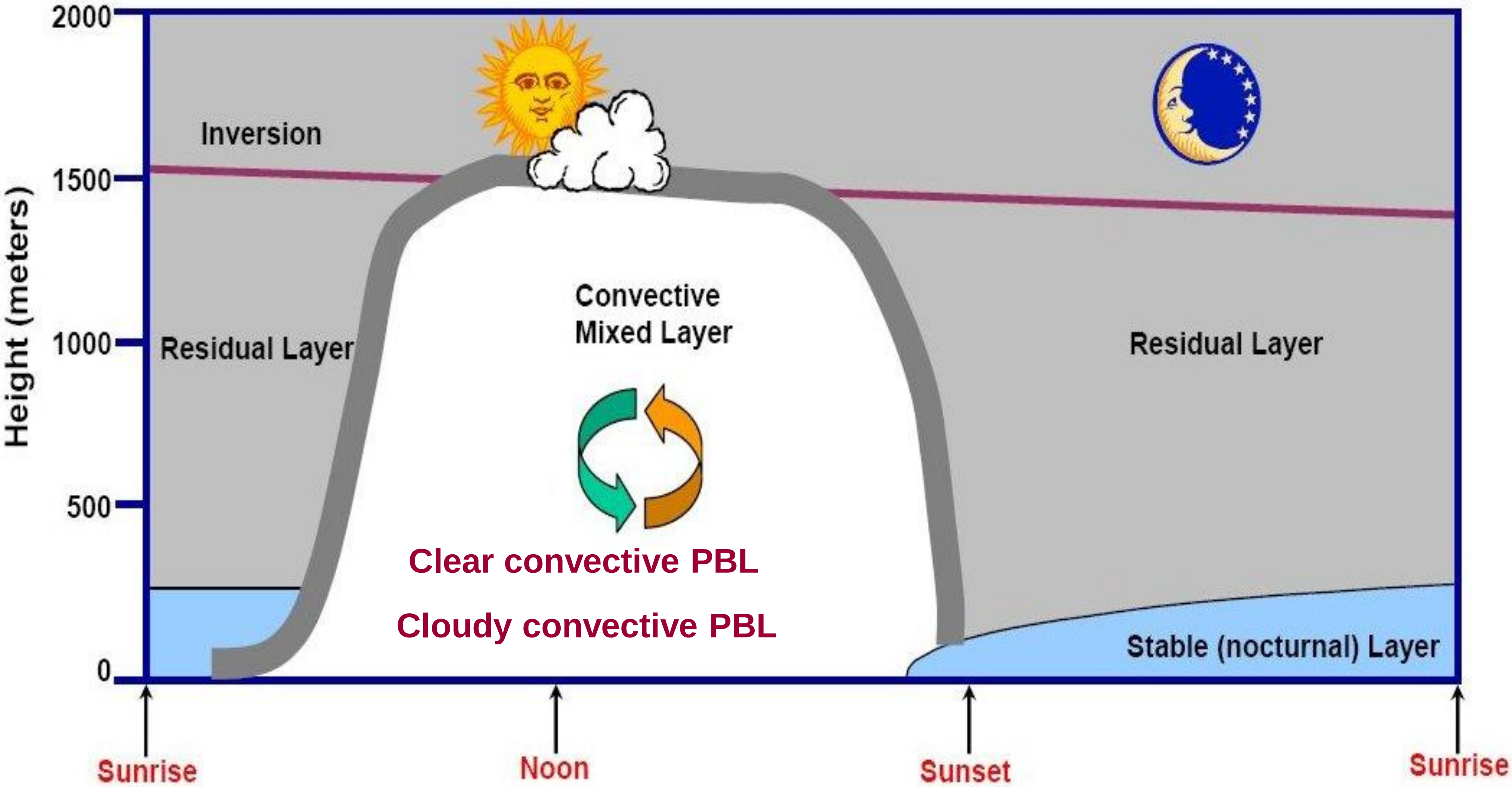
☞ Stable PBL:

- l << H (stability embeds turbulent motion)
- Turbulence is local (no influence from surface), stronger on horizontal
- Scaling : $(\overline{w'\theta'})_s$, $(\overline{u'w'})_s$, H

☞ Unstable (convective) PBL

- l ~ H (large eddies)
- Turbulence associated mostly to thermal production
- Turbulence is non-homogeneous and asymmetric (top-down, bottom-up)
- Scaling: H, $w_* = \left(\frac{g}{\overline{\theta}_v} (\overline{w'\theta'_v})_s H \right)^{1/3}$ → $\frac{z}{H}, q_* = \frac{E_0}{w_*}, \theta_* = \frac{Q_0}{w_*}$

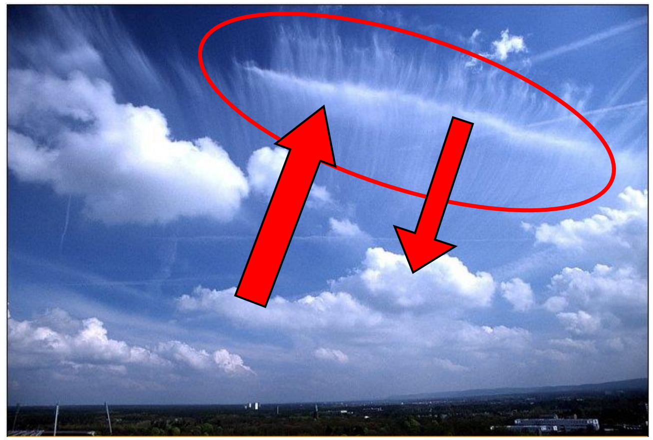
PBL: Diurnal variation



Adapted from **Introduction to Boundary Layer Meteorology** -R.B. Stull, 1988

Greenhouse effect : warming

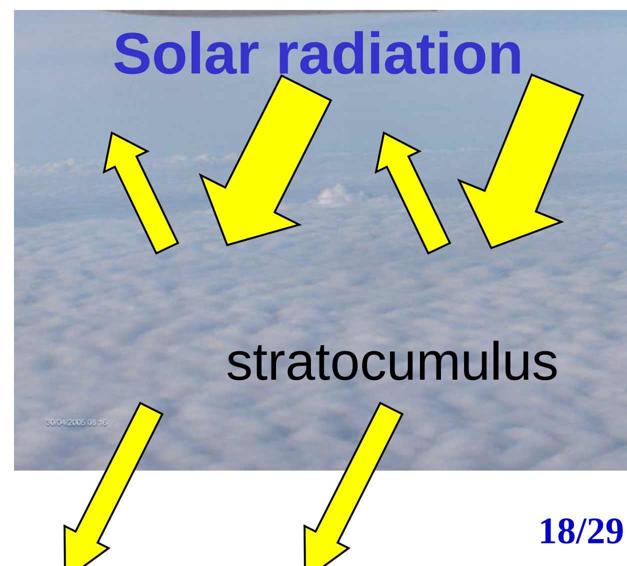
High clouds, like cirrus



Infrared radiation

Umbrella effect : cooling

Boundary layer clouds (low clouds)



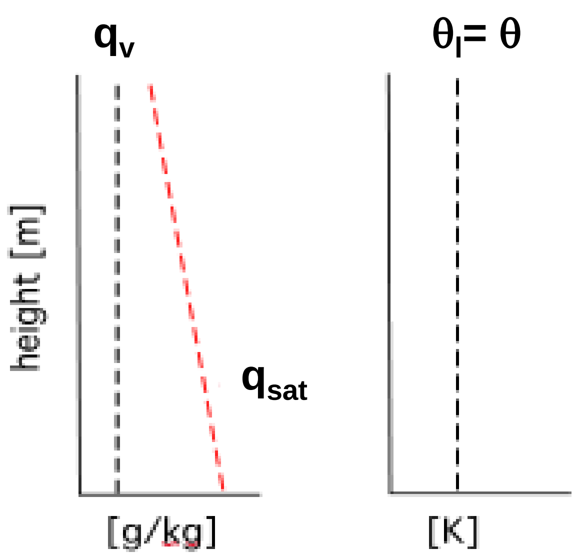
PBL: State variables

Clear PBL

Specific humidity $$q_v = \frac{m_v}{m_d + m_v}$$

Potential temperature $$\theta = T\left(\frac{p}{p_0}\right)^{-R_d / c_p}$$

no liquid water is condensed ($q_l = 0$)



Conserved variables

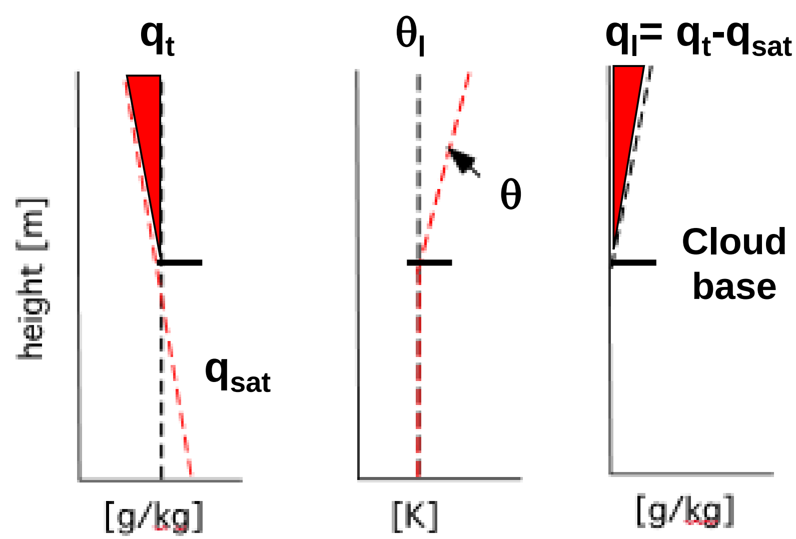
Cloudy PBL

Total water content $$q_t = \frac{m_v + m_c}{m_d + m_v + m_c}$$

Liquid water potential temperature $$\theta_l \approx \theta - \frac{L_v}{c_p} q_l$$

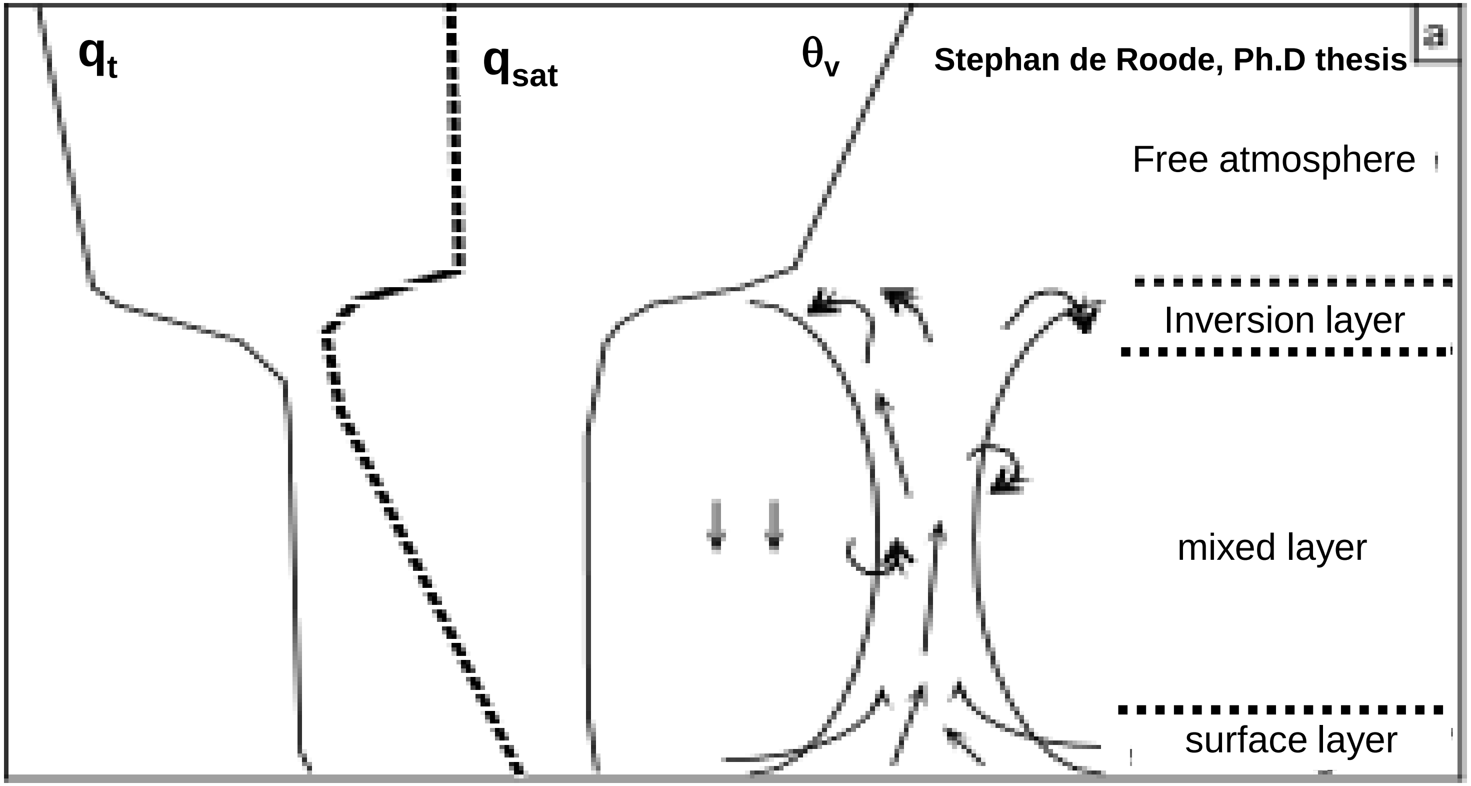
Evaporation temperature

liquid water is condensed

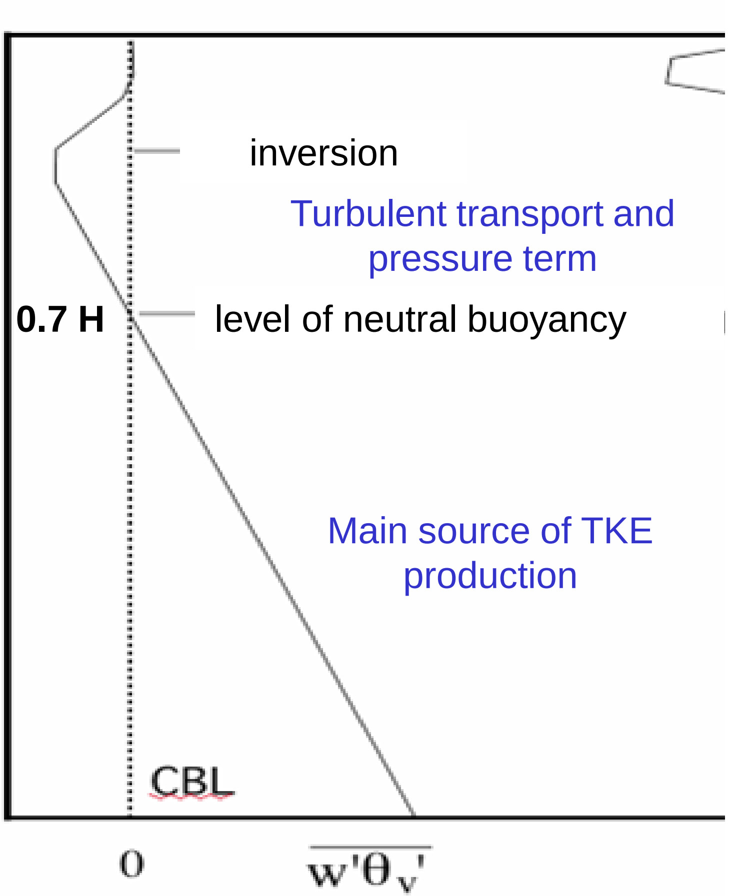


Conserved variables

Clear Convective PBL



☞ Buoyantly-driven from surface



☞ turbulent fluxes : a function of convective scaling variables: $\frac{z}{H}, q_* = \frac{E_0}{w_*}, \theta_* = \frac{Q_0}{w_*}$

☞ PBL height: $\frac{dH}{dt} = \overline{w} + w_e$

☞ Entrainment rate: (a possible parameterization) $w_e = A \frac{w_*^3}{\frac{g}{\theta_0} H \Delta\theta_v}$ with

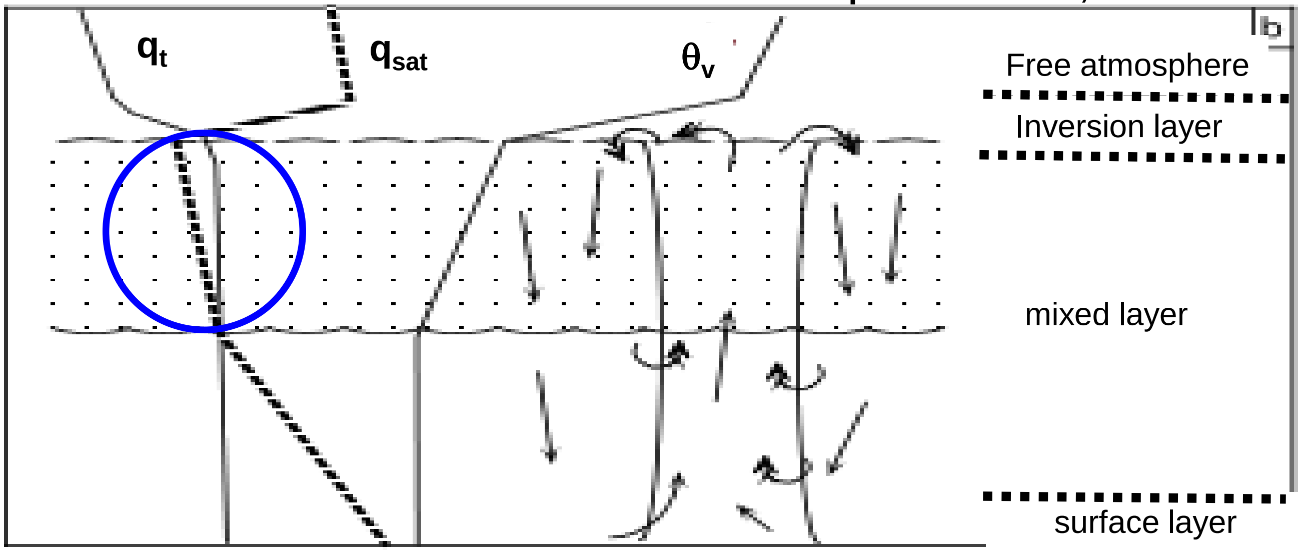
$$w_* = \left(\frac{g}{\overline{\theta}_v} (\overline{w'\theta_v'})_s H \right)^{1/3}$$

☞ Fluxes at PBL top: $\overline{w'\psi'}_H = -w_e \Delta\psi$

☞ Key parameters: $w_e, \Delta\theta_v, H, (\overline{w'\theta_v'})_0$

Cloudy boundary layers

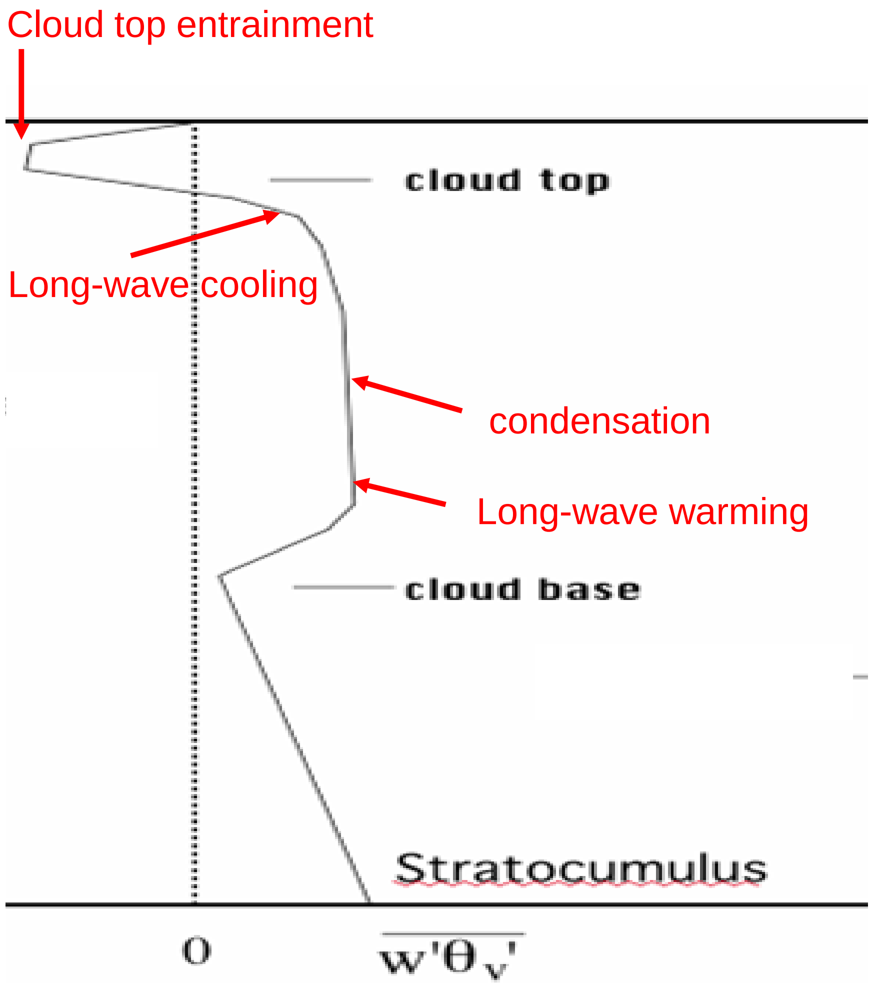
Stephan de Roode, Ph.D thesis



Stratocumulus topped PBL

Stratocumulus topped boundary layer

☞ Complicated turbulence structure



☞ Buoyantly driven by radiative cooling at cloud top

☞ Surface latent and heat flux play an important role

☞ Cloud top entrainment an order of magnitude stronger than in clear PBL

☞ Solar radiation transfer essential for the cloud evolution

☞ Key parameters: $w_e, \Delta\theta_v, H, \overline{(w'\theta_v')_0}$

$\overline{(w'q_v')_0}, \Delta q_t, z_b, \Delta F$

Cloudy boundary layers

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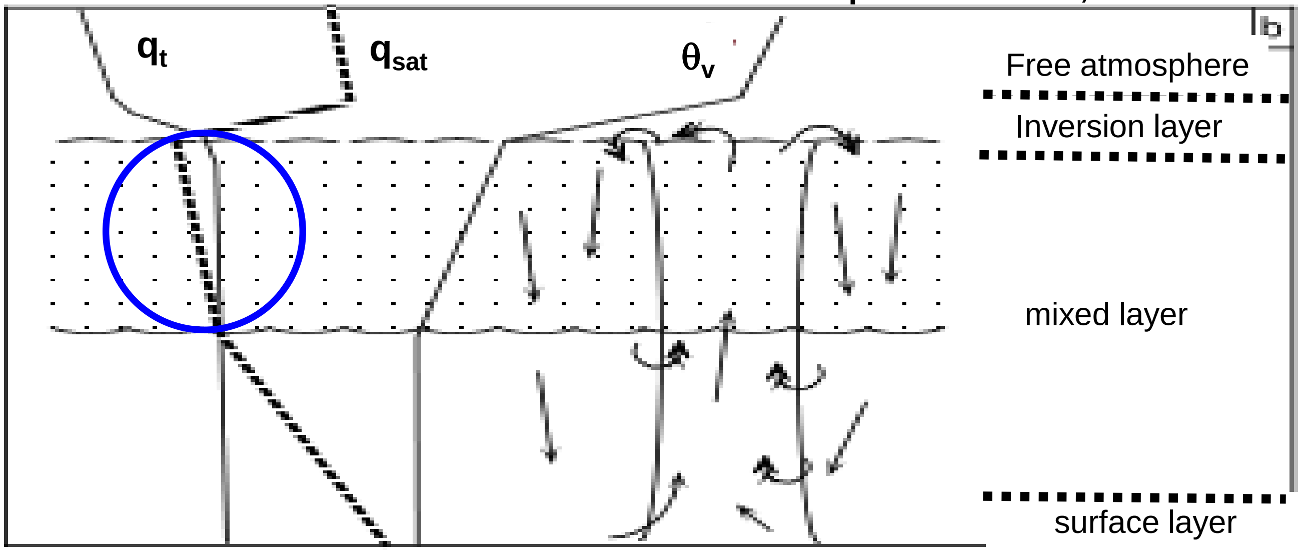
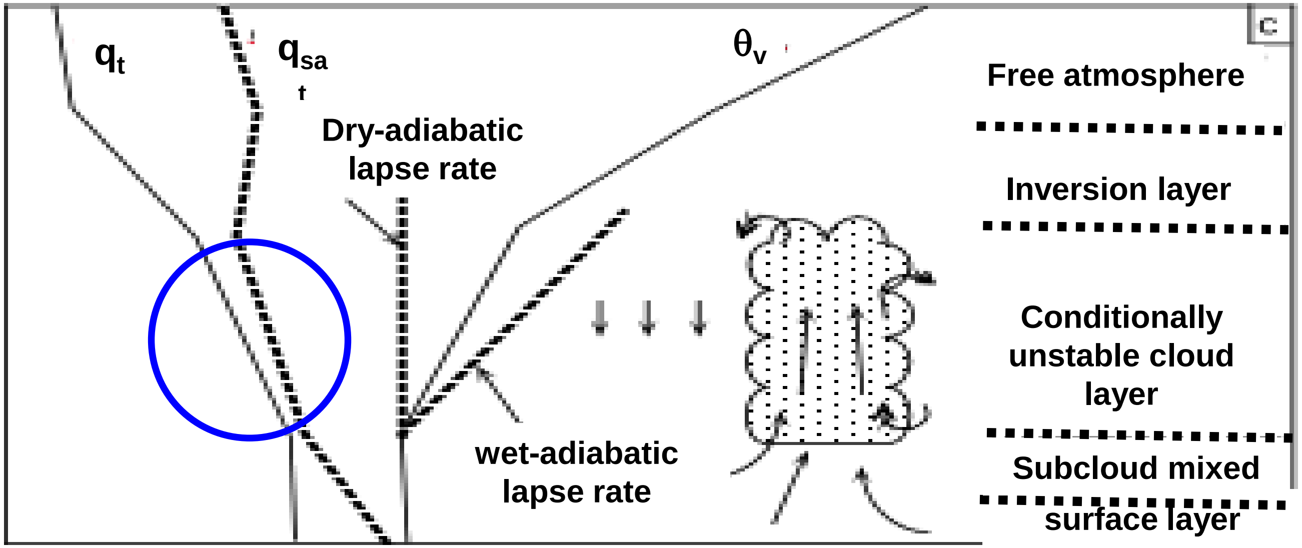


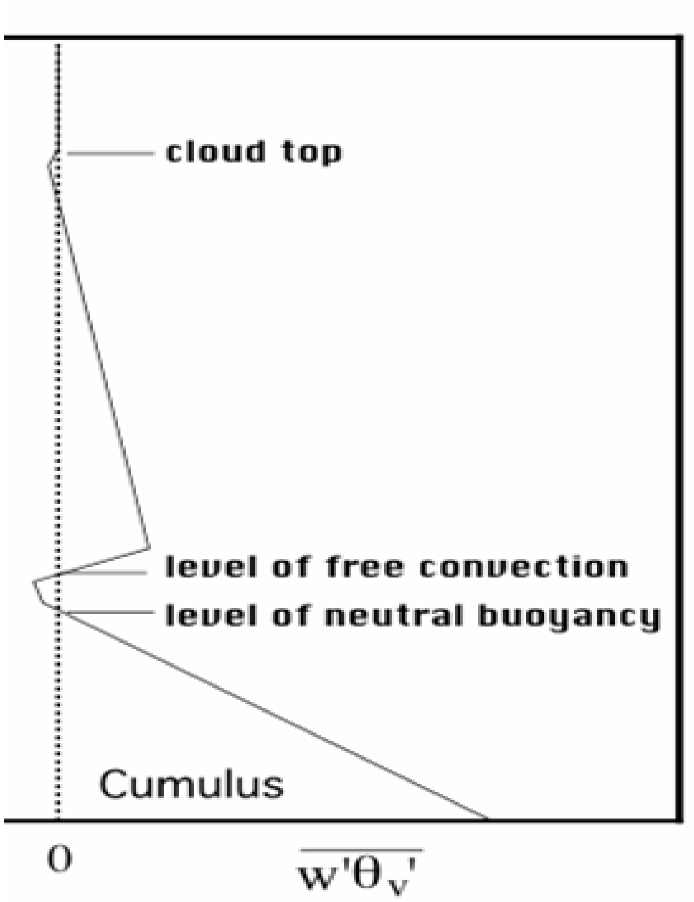
Stratocumulus topped PBL

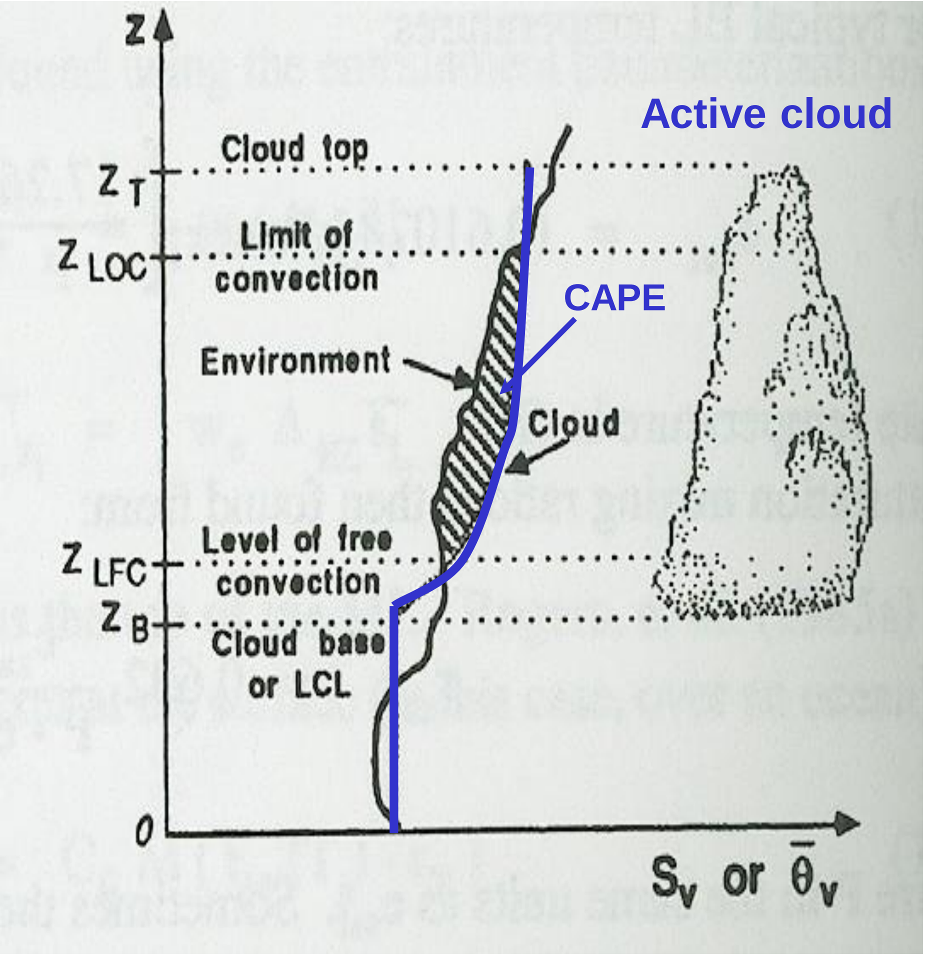


Cumulus PBL

Cumulus capped boundary layers

☞ Buoyancy is the main mechanism that forces cloud to rise





Cumulus capped boundary layers

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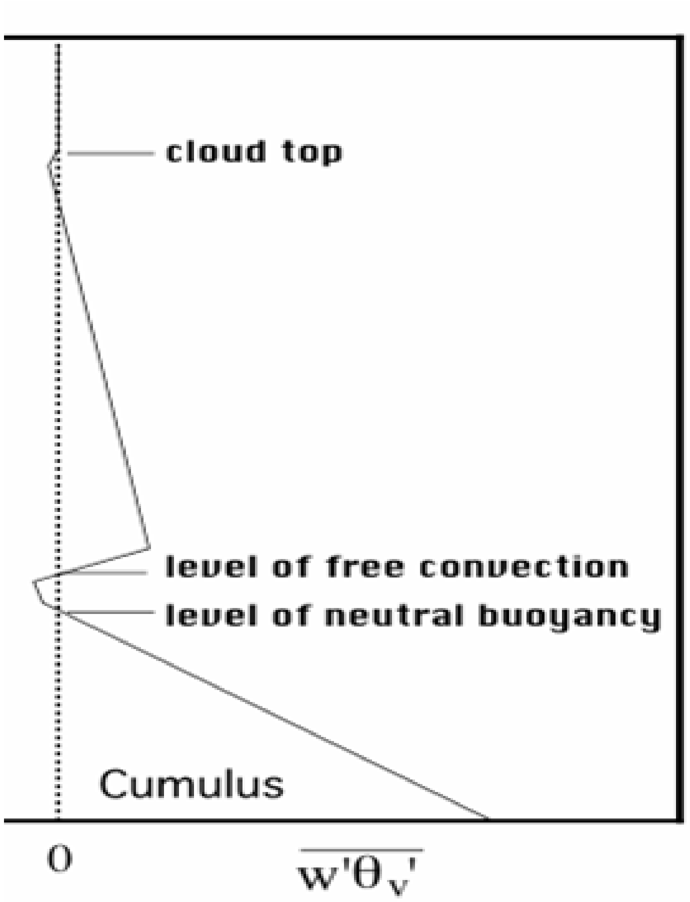

☞ Represented by mass flux convective schemes $M_c(\psi_u - \psi_d) = k\overline{w'\psi'}$

☞ Decomposition: cloud + environment

☞ Lateral entrainment/detrainment rates prescribed

☞ Key parameters: $H\,,\, z_b\,,\, \overline{(w'\theta_v')_0}\,,\, \overline{(w'q_v')_0}$

$$\left(\frac{\partial\theta_v}{\partial z}\right)_{environ.}, \left(\frac{\partial q_v}{\partial z}\right)_{environ.}$$

PBL: Summary

☞ Characteristics :

- ✘ several thousands of meters – 2-3 km above the surface
- ✘ turbulence, mixed layer
- ✘ convection
- ✘ Reynolds framework

☞ Classification:

- ✘ neutral (extremely rare)
- ✘ stable (nocturnal)
- ✘ convective (mostly diurnal)

☞ Clear convective

☞ Cloudy (stratocumulus or cumulus)

- ✘ Importance of boundary layer clouds (Earth radiative budget)
- ✘ Small liquid water contents, difficult to measure

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