

Observational bias correction in data assimilation

Niels Bormann, with material from
Hans Hersbach and Dick Dee

Meteorological Training Course
Data Assimilation

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Overview of this lecture

In this lecture we look at *observational biases*, and the variational bias correction scheme (VarBC) as used at ECMWF is explained.

VarBC replaced the tedious job of estimating observation bias *off-line* for each satellite instrument or in-situ network *with an automatic* self-adaptive *system*.

This is achieved by making the bias estimation an *integral part* of the ECMWF variational data *assimilation* system, where now both the initial model state and observation bias estimates are updated simultaneously.

By the end of the session you should be able to realize that:

1. Many observations are biased, and the *characteristics of bias vary widely* depending on the type of instrument,
2. *Distinguishing model bias from observation bias* is often difficult,
3. The success of an adaptive system implicitly relies on a *redundancy* in the underlying observing system.

Everyone knows that **models** are biased.

Not everyone knows that most **observations** are biased as well.

So... **where is the bias** term in this equation?

$$\mathbf{J}(\mathbf{x}) = \underbrace{(\mathbf{x}_b - \mathbf{x})^T \mathbf{B}^{-1} (\mathbf{x}_b - \mathbf{x})}_{\text{model background constraint}} + \underbrace{[\mathbf{y} - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{h}(\mathbf{x})]}_{\text{observational constraint}}$$

Bias: **mean(y-h(x))** (can be situation-dependent)

Outline

- Introduction
 - Biases in *models*, *observations*, and *observation operators*
 - Implications for *data assimilation*
- Variational analysis and correction of observation bias
 - The need for an adaptive system
 - Variational bias correction (VarBC)
- Limitations of VarBC

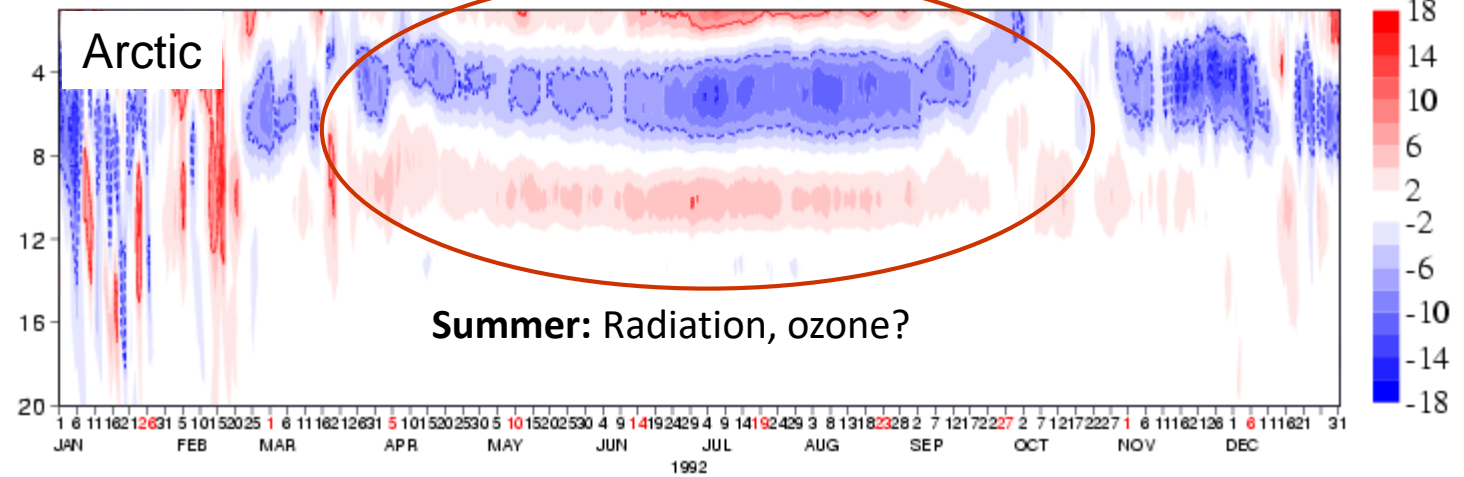
Model bias:

Seasonal variation in upper-stratospheric model errors

T255L60 model used for the *ERA-Interim* reanalysis

0.1hPa
(65km)

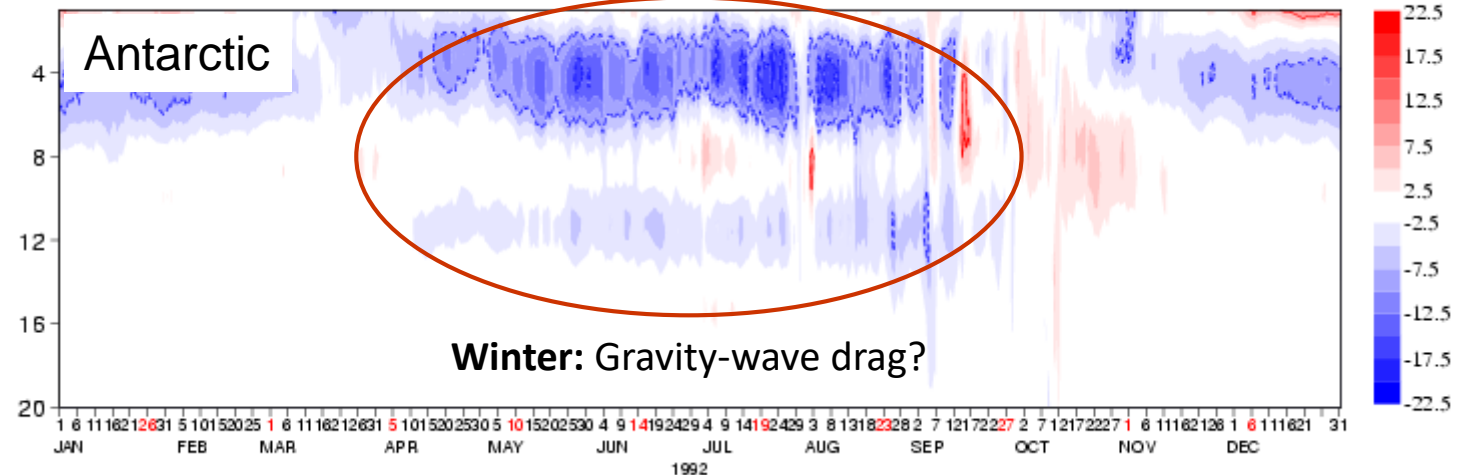
Mean temperature [K] 120-hour forecast errors for experiment 1112 : Arctic



40hPa
(22km)

0.1hPa
(65km)

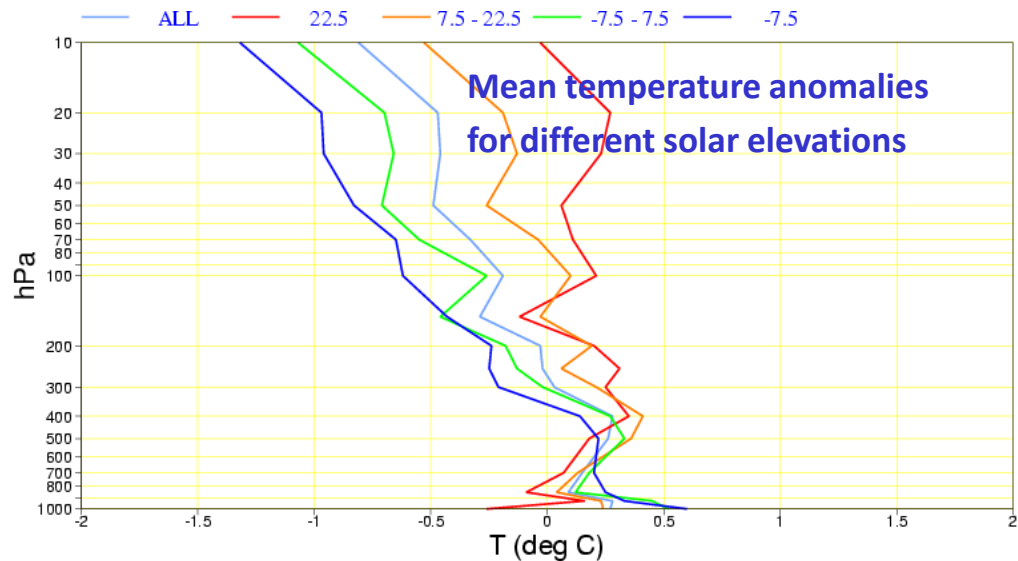
Mean temperature [K] 120-hour forecast errors for experiment 1112 : Antarctica



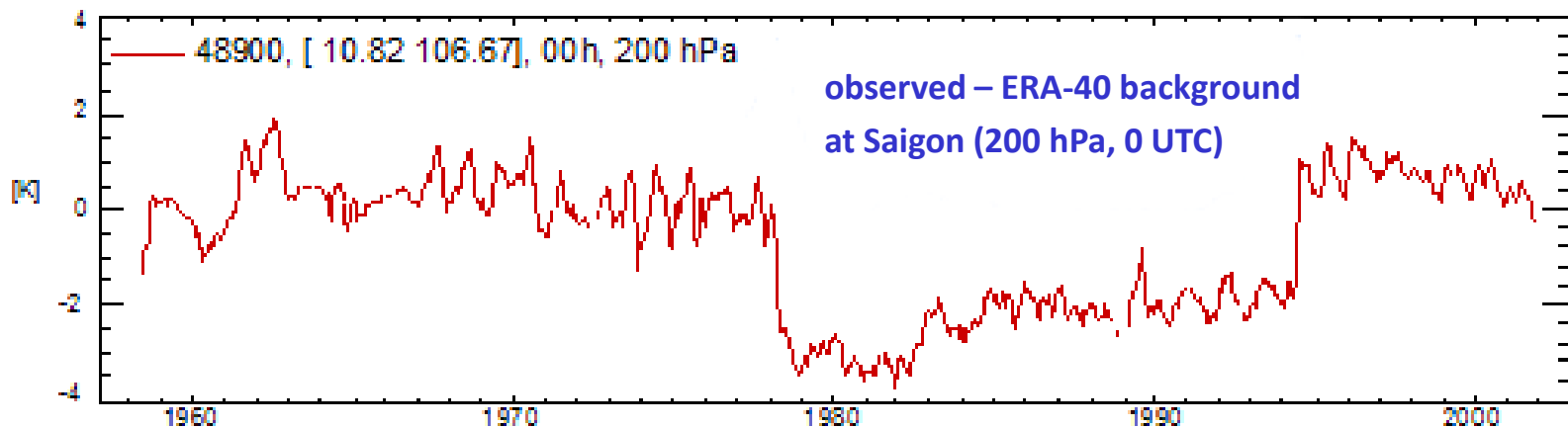
40hPa
(22km)

Observation bias: Radiosonde temperature observations

Daytime warm bias due to radiative heating of the temperature sensor
(depends on *solar elevation* and *equipment type*)



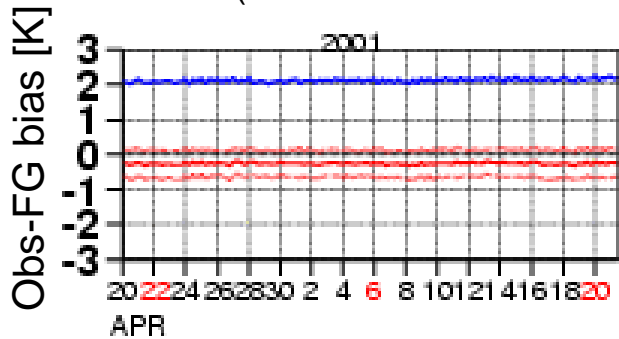
Bias changes due to change of equipment



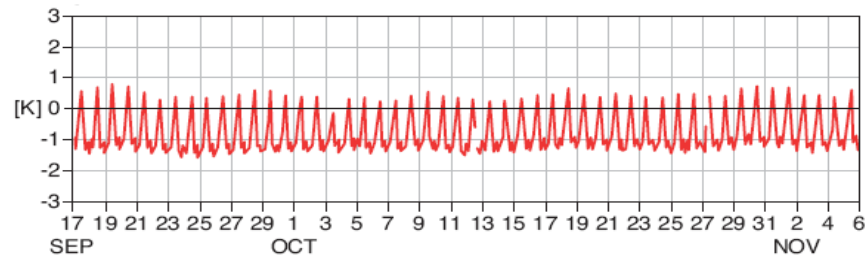
Observation and observation operator bias: Satellite radiances

Monitoring the background departures (averaged in time and/or space):

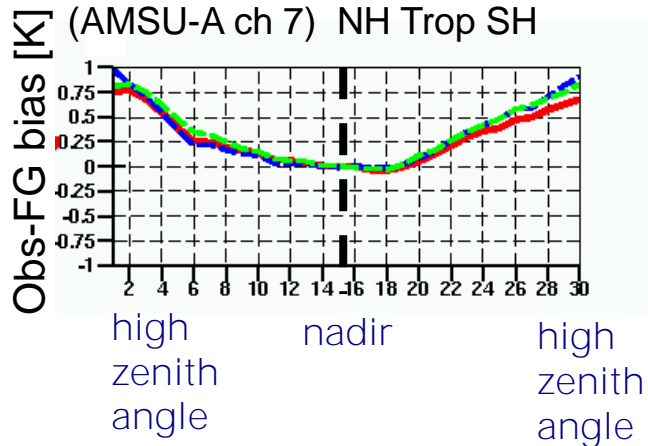
Constant bias (NOAA-14 HIRS channel 5)



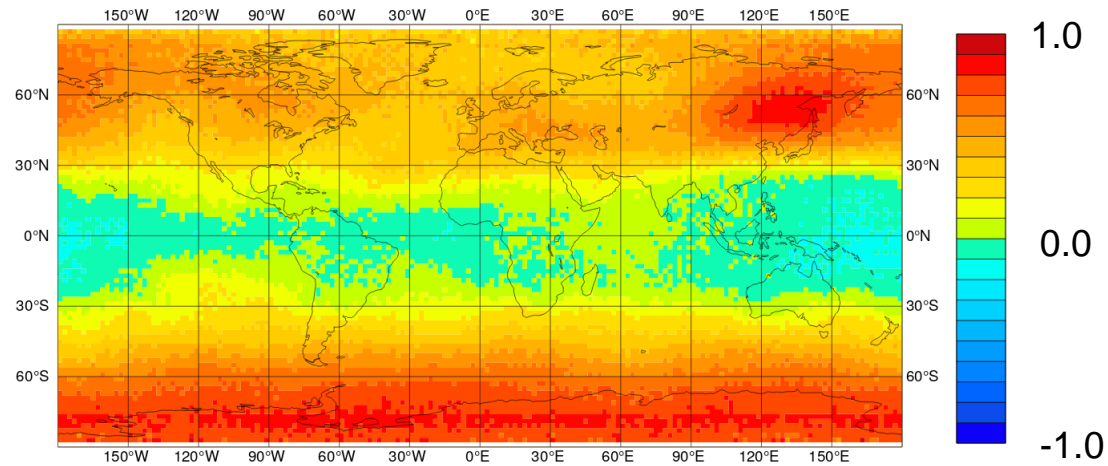
Diurnal bias variation in a geostationary satellite



Bias depending on scan position
(AMSU-A ch 7) NH Trop SH

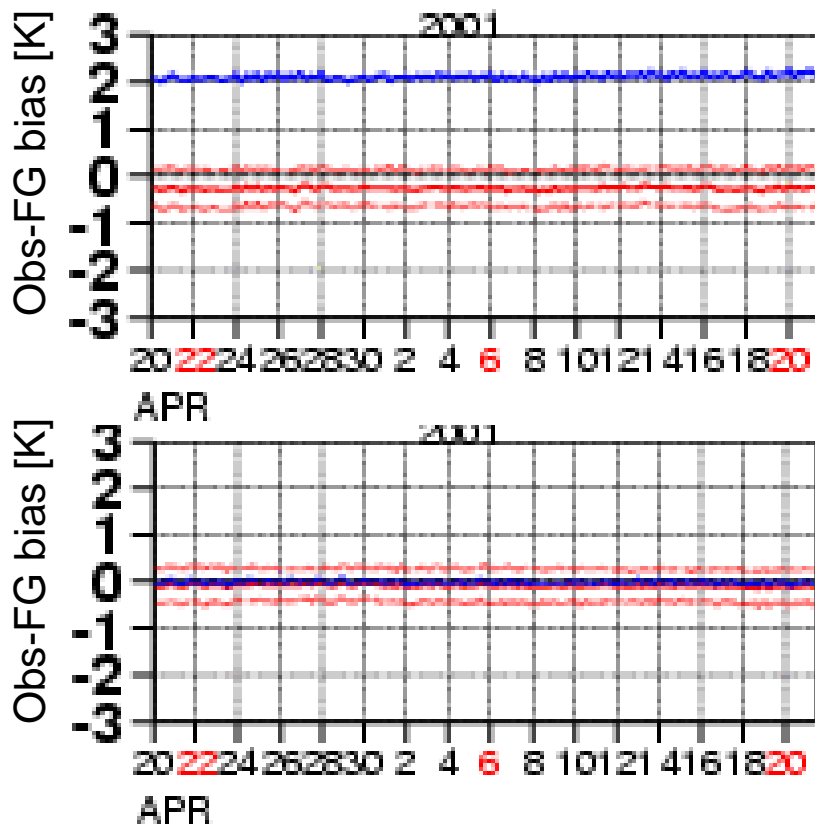


Air-mass dependent bias (AMSU-A ch 8)



Observation and observation operator bias: Satellite radiances – sources of bias

Monitoring the background departures (averaged in time and/or space):



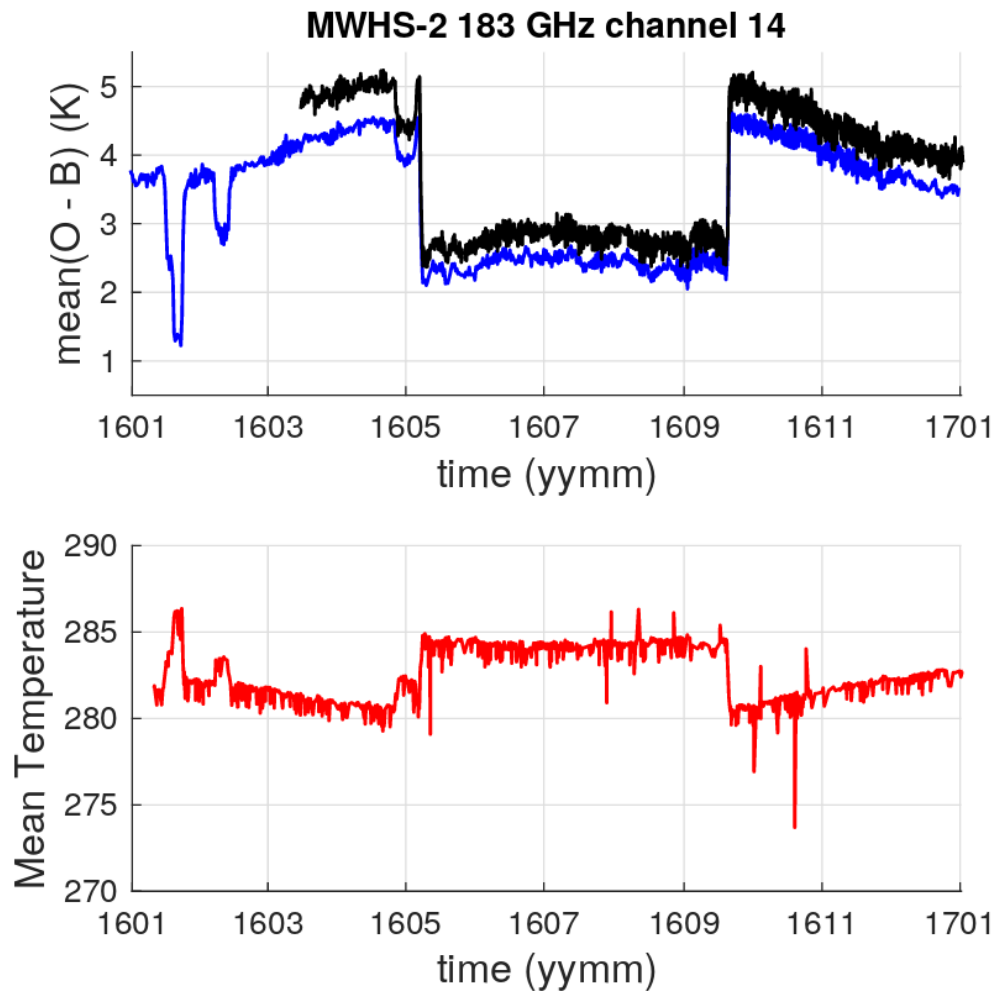
HIRS channel 5 (peaking around 600hPa) on **NOAA-14** satellite has +2.0K radiance bias against FG.

Same channel on **NOAA-16** satellite has no radiance bias against FG.

→ NOAA-14 channel 5 has an instrument bias.

Observation and observation operator bias: Satellite radiances – sources of bias

A time-varying bias, apparently dependent on the temperature of the satellite instrument:



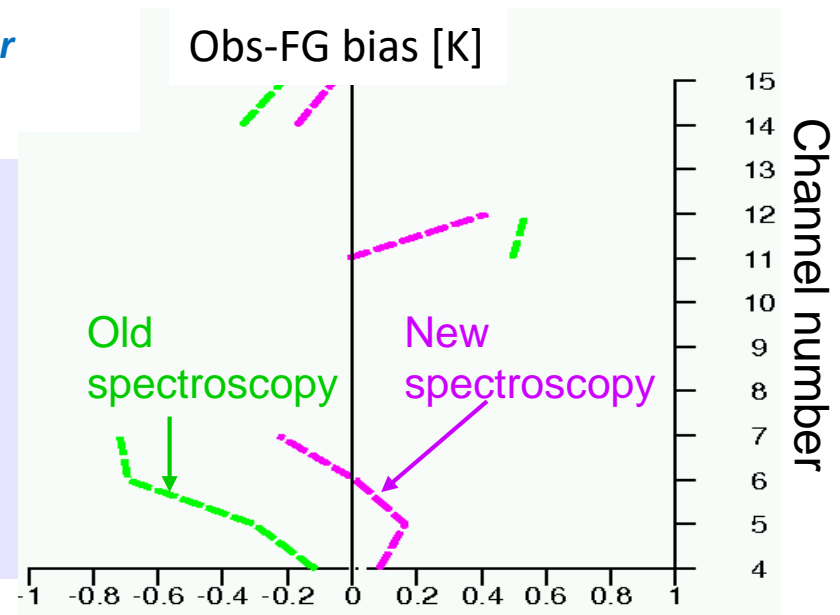
— ECMWF MWHS-2 — Met Office MWHS-2 — Mean Instrument Environment Temperature

Observation and observation operator bias: Satellite radiances – sources of bias

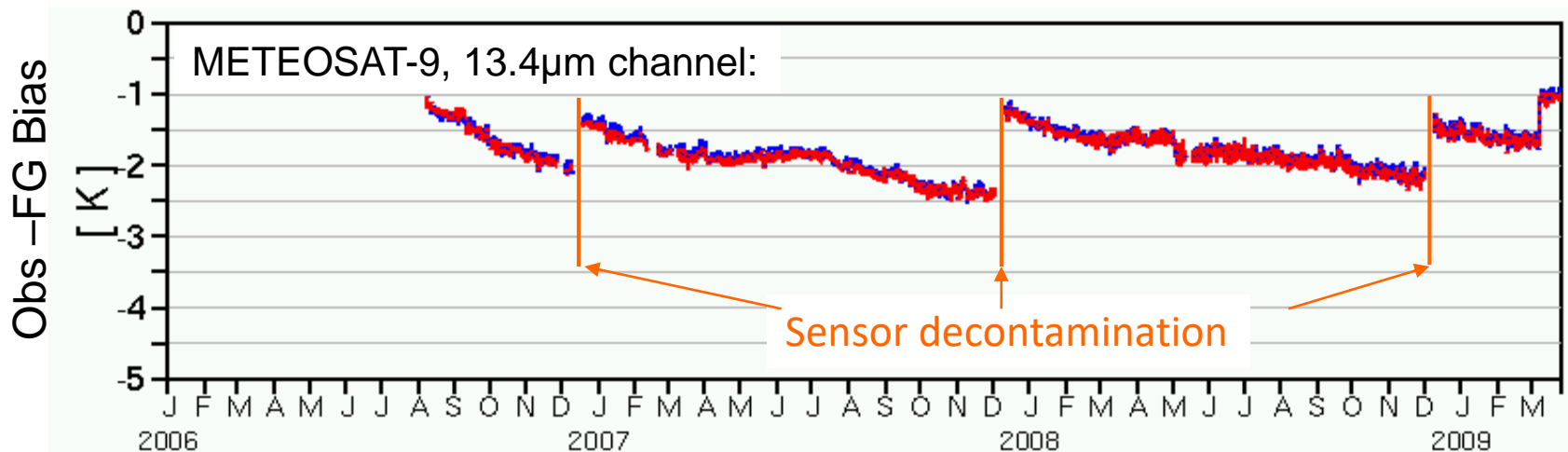
Different spectroscopy in the *radiative transfer model* can lead to different bias, e.g. for HIRS:

Other common causes for biases in radiative transfer:

- Bias in assumed concentrations of atmospheric gases (e.g., CO₂, aerosols)
- Neglected effects (e.g., clouds)
- Incorrect spectral response function
-



Drift in bias due to ice-build up on sensor:

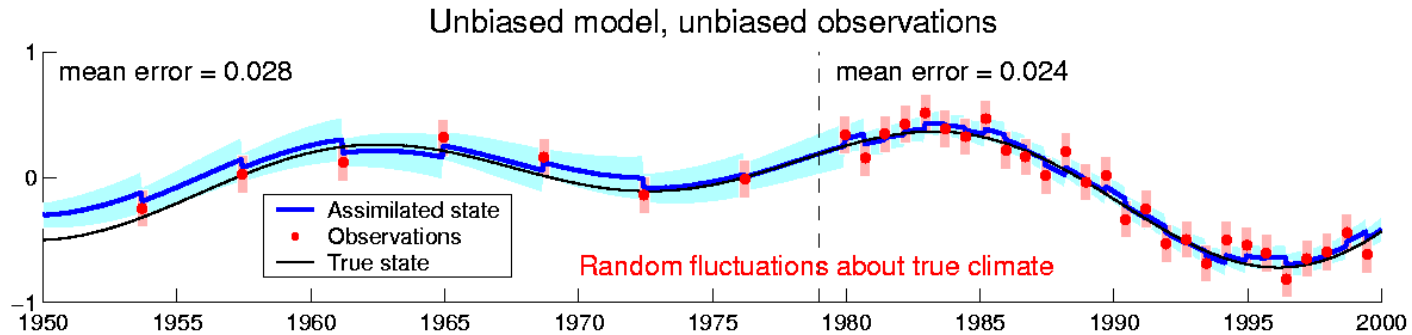


Implications for data assimilation: Bias problems in a nutshell

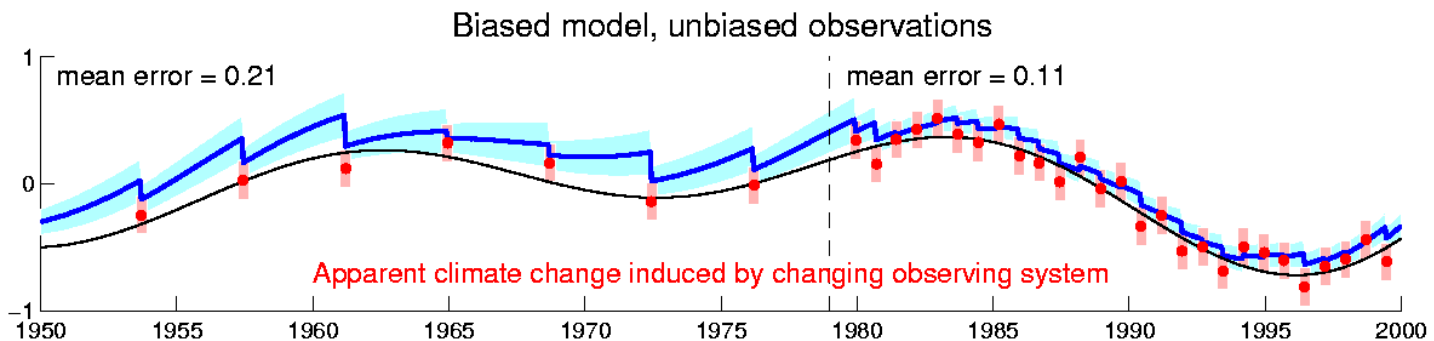
- **Observations** and observation operators have biases, which may change over time
 - Daytime warm bias in radiosonde measurements of stratospheric temperature; radiosonde equipment changes
 - Biases in satellite radiance measurements and radiative transfer models
 - Biases in cloud-drift wind data due to problems in height assignment
- **Models** have biases, and changes in observational coverage over time may change the extent to which observations correct these biases
 - Stratospheric temperature bias modulated by radiance assimilation
 - This is especially important for reanalysis (trend analysis)
- **Data assimilation** methods are primarily designed to correct *small random errors* in the model background
 - Systematic inconsistencies among different parts of the observing system lead to all kinds of problems

Implications for data assimilation: The effect of model bias on trend estimates

Most assimilation systems assume unbiased models and unbiased data



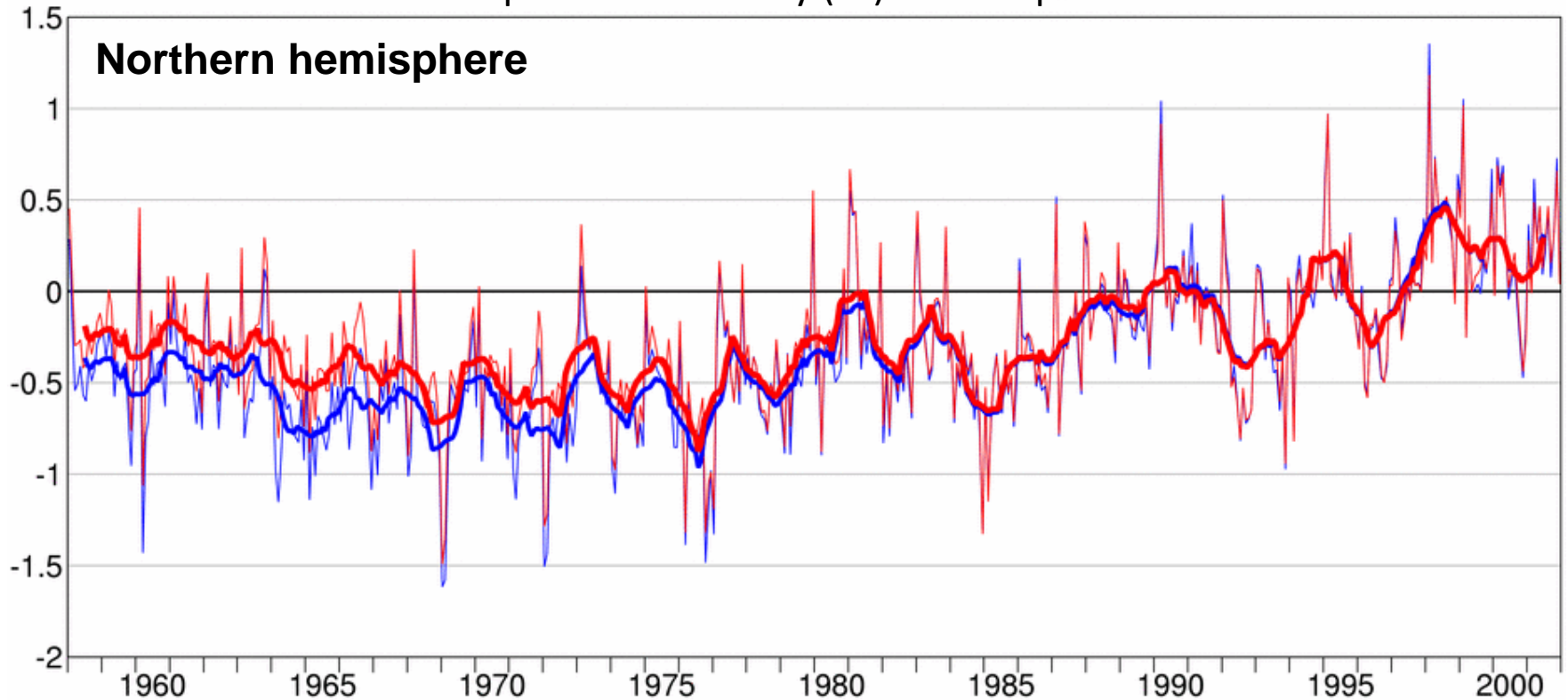
Biases in models and/or data can induce spurious trends in the assimilation



Implications for data assimilation:

ERA-40 surface temperatures compared to land-station values

Surface air temperature anomaly ($^{\circ}\text{C}$) with respect to 1987-2001



Based on monthly CRUTEM2v data (Jones and Moberg, 2003)

Based on ERA-40 reanalysis

Outline

- Introduction
 - Biases in models, observations, and observation operators
 - Implications for data assimilation
- Variational analysis and correction of observation bias
 - The need for an *adaptive* system
 - The variational bias correction scheme: *VarBC*
- Limitations of VarBC

Variational analysis and bias correction: A brief review of variational data assimilation

$$\text{Minimise } \mathbf{J}(\mathbf{x}) = \underbrace{(\mathbf{x}_b - \mathbf{x})^T \mathbf{B}^{-1} (\mathbf{x}_b - \mathbf{x})}_{\text{background constraint } (\mathbf{J}_b)} + \underbrace{[\mathbf{y} - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{h}(\mathbf{x})]}_{\text{observational constraint } (\mathbf{J}_o)}$$

- The input \mathbf{x}_b represents past information propagated by the forecast model
(the **model background**)
- The input $[\mathbf{y} - \mathbf{h}(\mathbf{x}_b)]$ represents the new information entering the system
(the **background departures**)
- The function $\mathbf{h}(\mathbf{x})$ represents a model for simulating observations
(the **observation operator**)
- Minimising the cost function $\mathbf{J}(\mathbf{x})$ produces an adjustment to the model background based on all used observations
(the **analysis**)

Variational analysis and bias correction: Error sources in the input data

$$\text{Minimise } \mathbf{J}(\mathbf{x}) = \underbrace{(\mathbf{x}_b - \mathbf{x})^T \mathbf{B}^{-1} (\mathbf{x}_b - \mathbf{x})}_{\text{background constraint } (\mathbf{J}_b)} + \underbrace{[\mathbf{y} - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{h}(\mathbf{x})]}_{\text{observational constraint } (\mathbf{J}_o)}$$

- **Errors in the input $[\mathbf{y} - \mathbf{h}(\mathbf{x}_b)]$ arise from:**
 - errors in the actual observations
 - errors in the model background
 - errors in the observation operator
- **There is no general method for separating these different error sources**
 - we only have information about differences
 - there is no true reference in the real world!
- **The analysis does not respond well to conflicting input information**

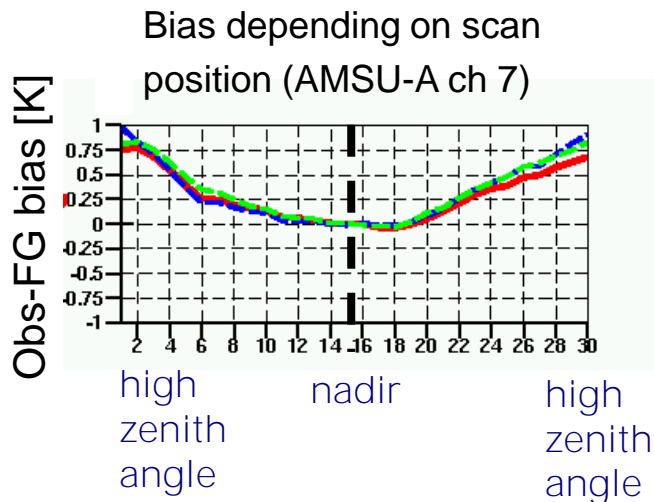
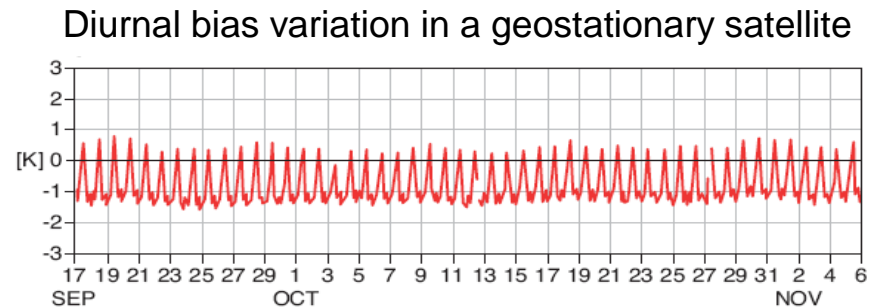
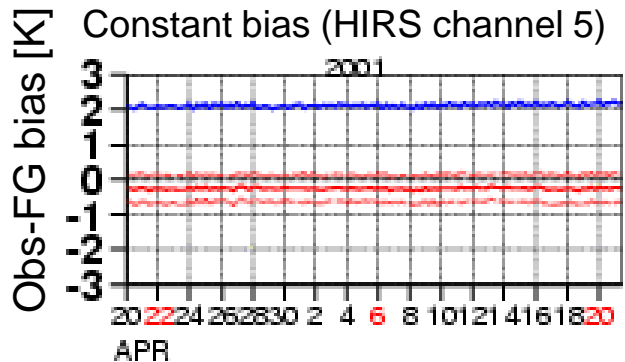
A lot of work is done to remove biases prior to assimilation:

 - ideally by removing the cause
 - in practise by careful comparison against other data

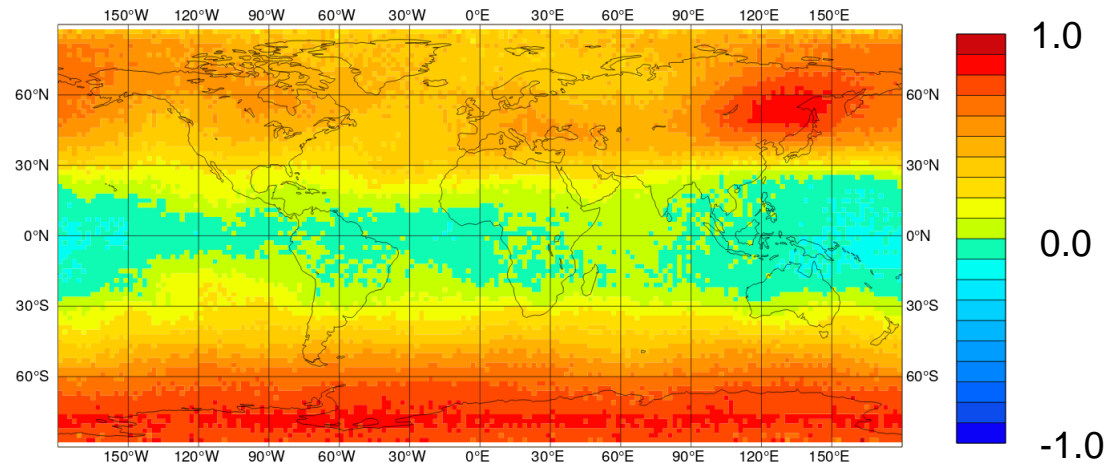
The need for an adequate bias model

Prerequisite for any bias correction is a good model for the bias ($b(x, \beta)$):

- Ideally, guided by the physical origins of the bias.
- In practice, bias models are derived empirically from observation monitoring.



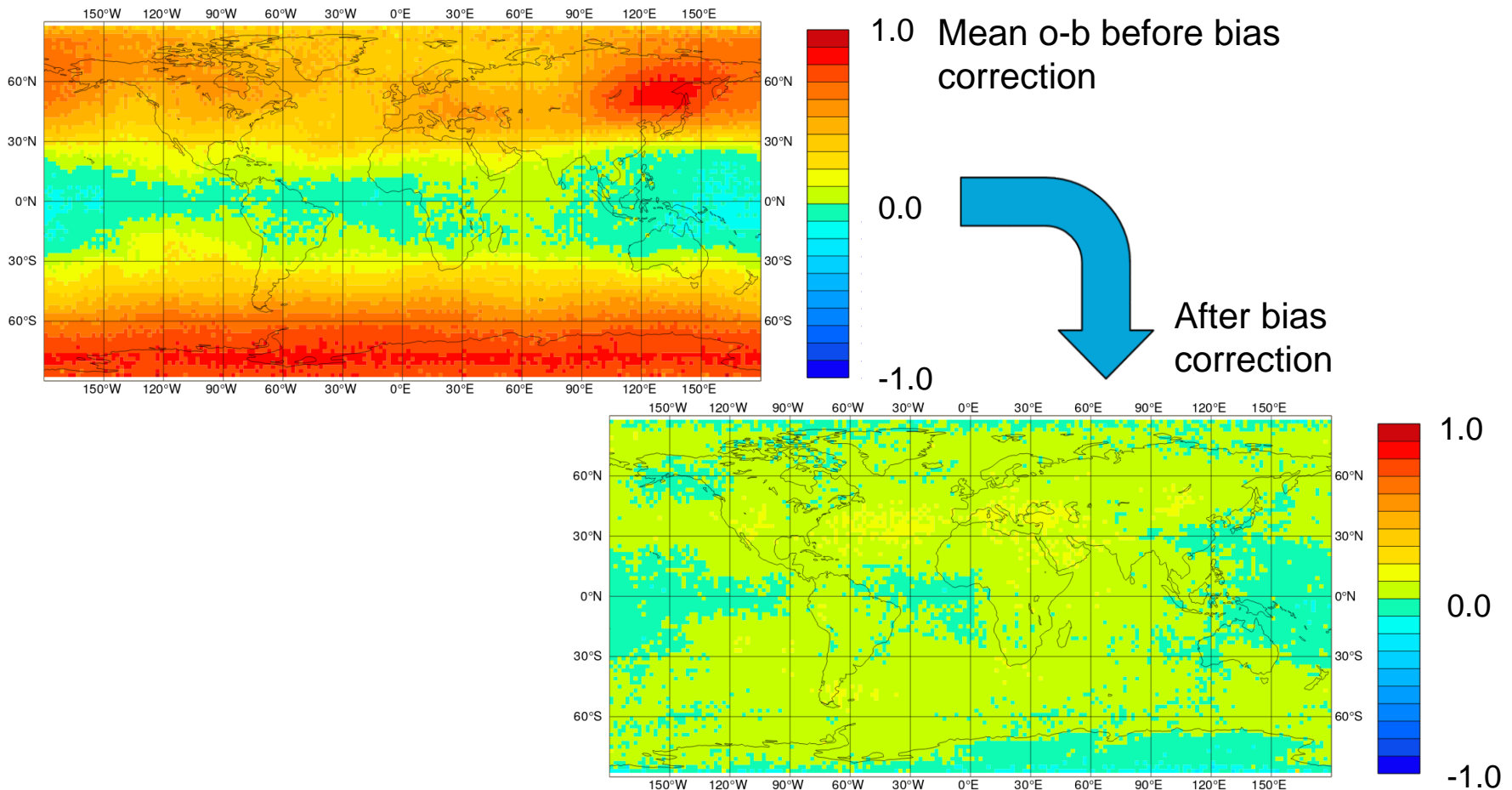
Air-mass dependent bias (AMSU-A ch 8)



The need for an adequate bias model

Prerequisite for any bias correction is a good model for the bias ($b(\mathbf{x}, \boldsymbol{\beta})$):

- For instance, a linear model with some predictors p_1, p_2, \dots, p_n , and free parameters $\beta_0, \beta_1, \beta_2, \dots, \beta_n$: $b(\mathbf{x}, \boldsymbol{\beta}) = \beta_0 + \beta_1 p_1 + \beta_2 p_2 + \dots + \beta_n p_n$
- Avoid models with too many free parameters.



Satellite radiance bias correction at ECMWF, prior to 2006

Scan bias and **air-mass dependent bias** for each satellite/sensor/channel were estimated off-line from background departures, and stored in files (**Harris and Kelly 2001**)

Error model for brightness temperature data: $y = h(x) + b^{scan} + b^{air}(x) + e^{obs}$

where $b^{scan} = b^{scan}(\text{latitude, scan position})$

$$b^{air} = \beta_0 + \sum_{i=1}^N \beta_i p_i(x)$$

e^{obs} = random observation error

Predictors, for instance:

- 1000-300 hPa thickness
- 200-50 hPa thickness
- surface skin temperature
- total precipitable water

Average the background departures:

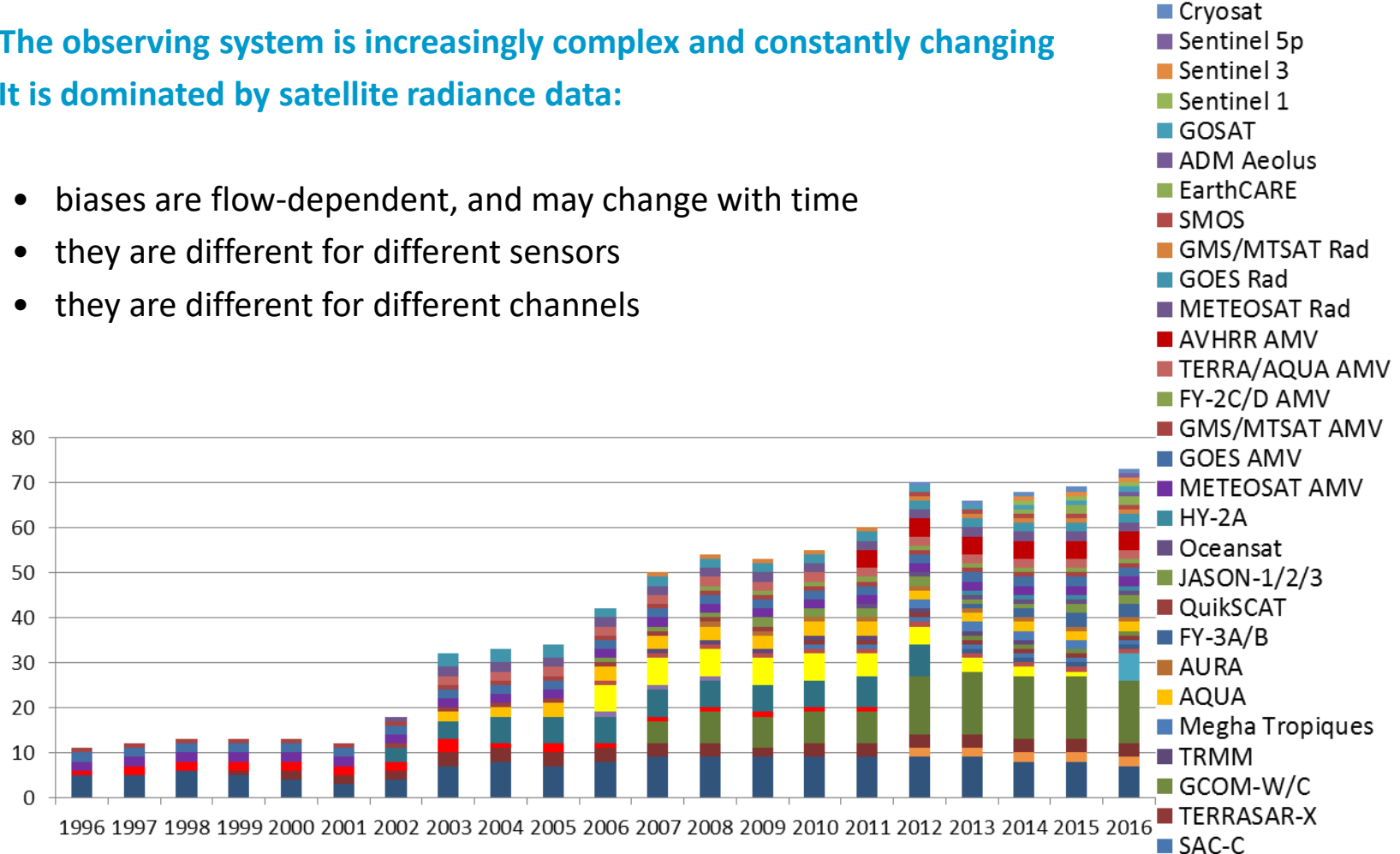
$$\langle y - h(x_b) \rangle = b^{scan} + b^{air}(x)$$

Periodically estimate scan bias and predictor coefficients:

- typically 2 weeks of background departures
- 2-step regression procedure
- careful masking and data selection

The need for an adaptive bias correction system

- **The observing system is increasingly complex and constantly changing**
- **It is dominated by satellite radiance data:**
 - biases are flow-dependent, and may change with time
 - they are different for different sensors
 - they are different for different channels



- **How can we manage the bias corrections for all these different components?**
- **This requires a consistent approach and a flexible, automated system**

The Variational Bias Correction scheme:

The general idea

The **bias** in a given instrument/channel (**bias group**) is described by (a few) **bias parameters**: typically, these are functions of air-mass and scan-position (the **predictors**)

These parameters can be estimated in a variational analysis along with the model state (**Derber and Wu, 1998 at NCEP, USA**)

The **standard variational analysis** minimizes

$$J(x) = (x_b - x)^T B_x^{-1} (x_b - x) + [y - h(x)]^T R^{-1} [y - h(x)]$$



Modify the observation operator to account for bias: $\tilde{h}(z) = \tilde{h}(x, \beta)$

Include the bias parameters in the control vector: $z^T = [x^T \quad \beta^T]$

Minimize instead

$$J(z) = (z_b - z)^T B_z^{-1} (z_b - z) + [y - \tilde{h}(z)]^T R^{-1} [y - \tilde{h}(z)]$$

What is needed to implement this:

1. The modified operator $\tilde{h}(x, \beta)$ and its TL + adjoint
2. A cycling scheme for updating the bias parameter estimates
3. An effective preconditioner for the joint minimization problem

Variational bias correction: The modified analysis problem

The original problem:

\mathbf{J}_b : background constraint

$$J(\mathbf{x}) = (\mathbf{x}_b - \mathbf{x})^T \mathbf{B}^{-1} (\mathbf{x}_b - \mathbf{x}) + \underbrace{[\mathbf{y} - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{h}(\mathbf{x})]}_{\mathbf{J}_o: \text{observation constraint}}$$

The modified problem:

\mathbf{J}_b : background constraint for \mathbf{x} \mathbf{J}_β : background constraint for β

$$\mathbf{J}(\mathbf{x}, \beta) = (\mathbf{x}_b - \mathbf{x})^T \mathbf{B}_x^{-1} (\mathbf{x}_b - \mathbf{x}) + \underbrace{(\beta_b - \beta)^T \mathbf{B}_\beta^{-1} (\beta_b - \beta)}_{\mathbf{J}_\beta: \text{background constraint for } \beta} + \underbrace{[\mathbf{y} - \mathbf{b}_o(\mathbf{x}, \beta) - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{b}_o(\mathbf{x}, \beta) - \mathbf{h}(\mathbf{x})]}_{\mathbf{J}_o: \text{bias-corrected observation constraint}}$$

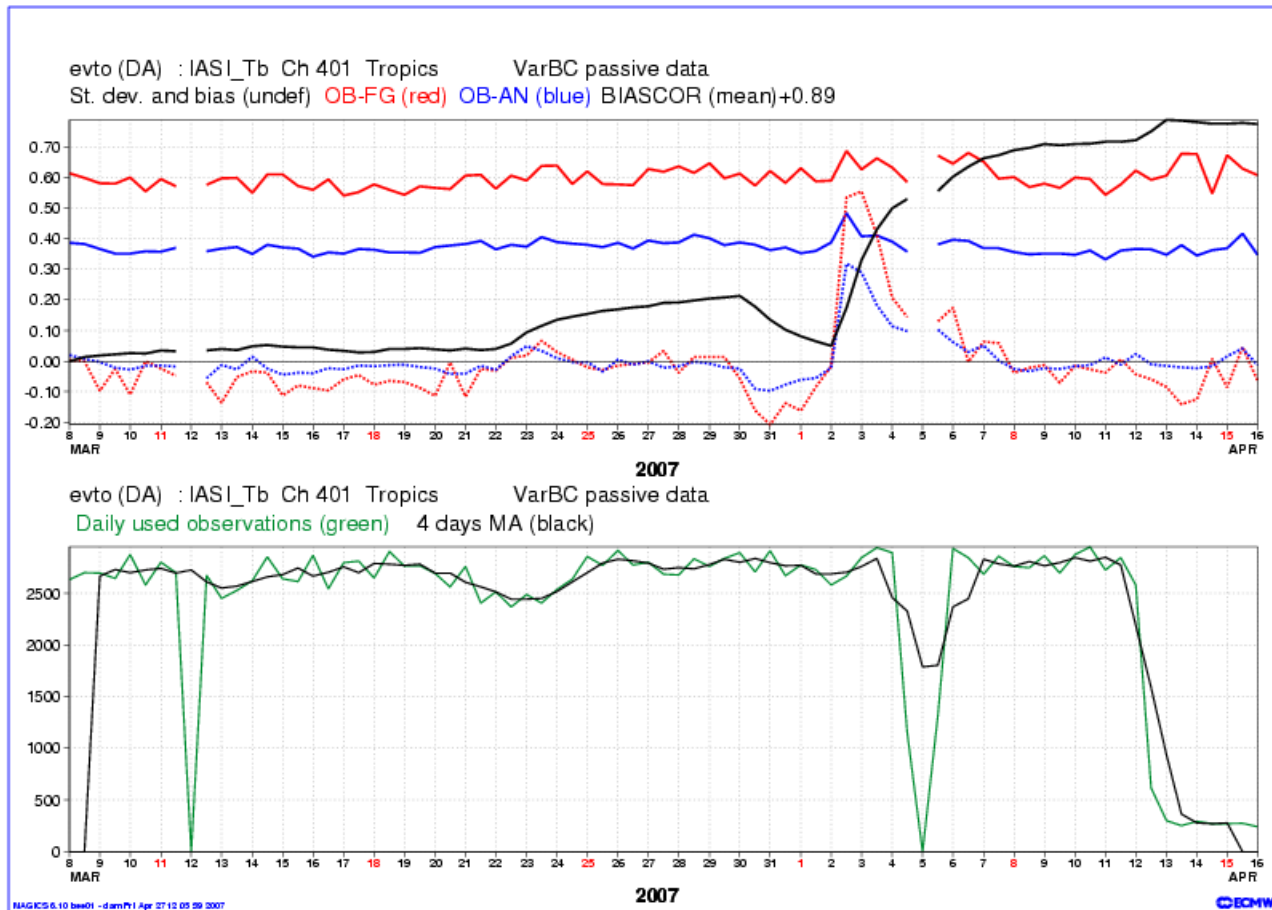
Parameter estimates from previous analysis

A model for the observation bias

Example 1:

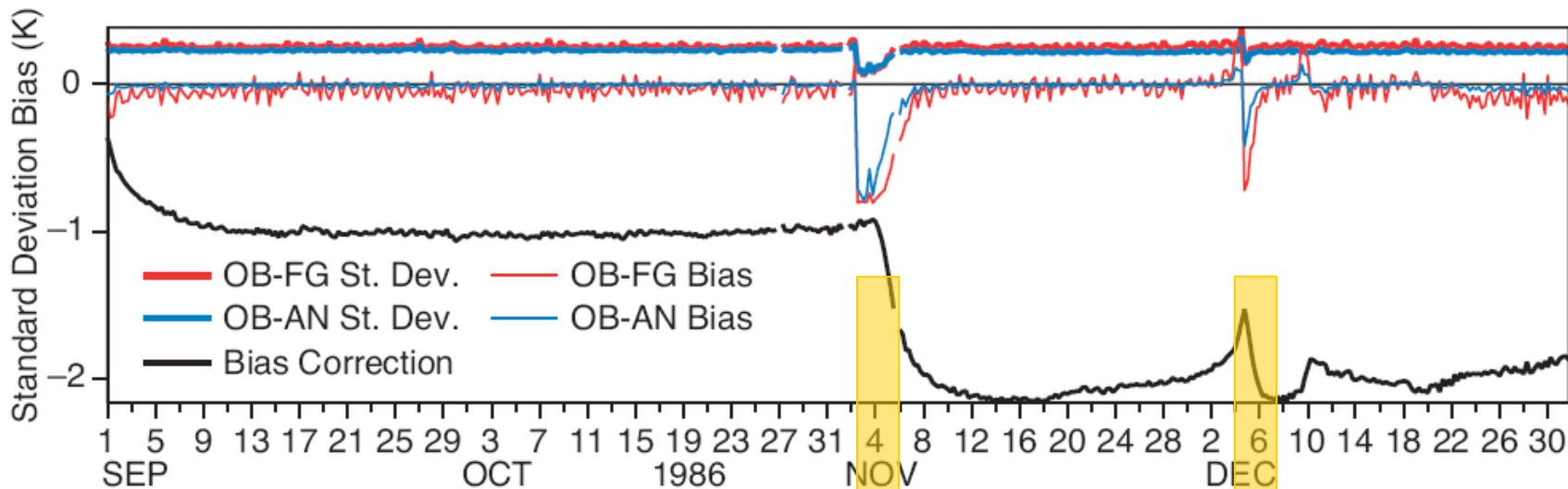
Spinning up new instruments – IASI on MetOp A

- IASI is a high-resolution interferometer with 8461 channels
- Initially unstable – data gaps, preprocessing changes

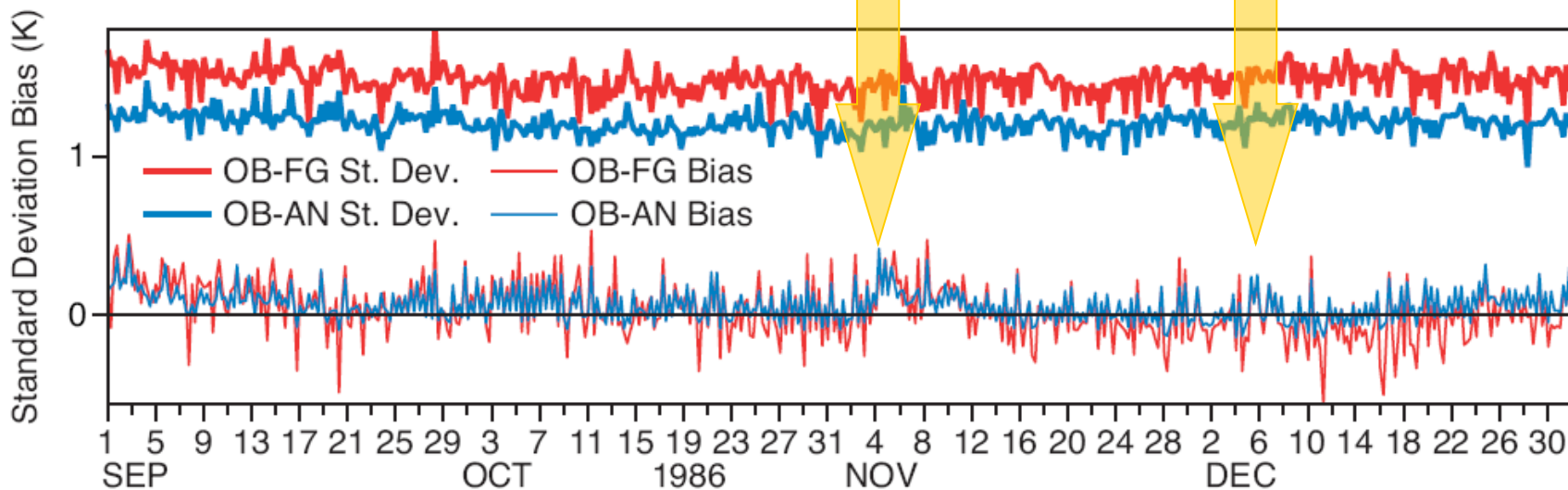


Example 2:

NOAA-9 MSU channel 3 bias corrections (cosmic storm)

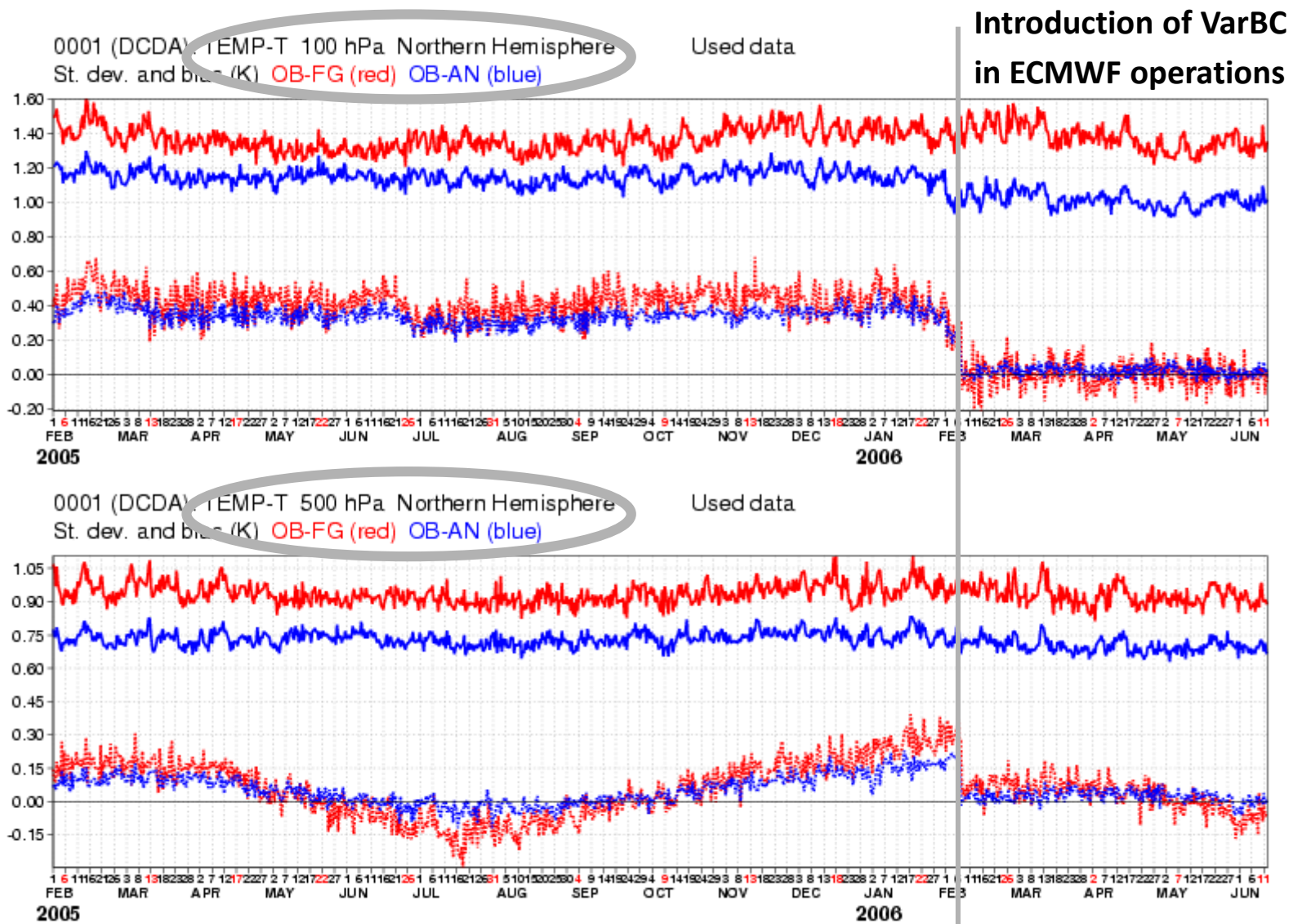


200 hPa temperature departures from radiosonde observations



Example 3:

Fit to conventional data



Bias correction use at ECMWF

Current VarBC bias 'classes' in the ECMWF operational system:

- *Radiances*
- *Ozone*
- *Aircraft data*
- *Ground-based radar precipitation*

Other automated bias corrections, but outside 4D-Var:

- Surface pressure
- Radiosonde temperature and humidity
- Soil moisture (in SEKF surface analysis)

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Limitations of VarBC: Interaction with model bias

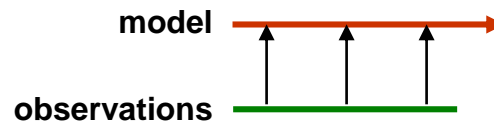
VarBC introduces extra degrees of freedom in the variational analysis, to help improve the fit to the (bias-corrected) observations:

$$\mathbf{J}(\mathbf{x}, \boldsymbol{\beta}) = (\mathbf{x}_b - \mathbf{x})^T \mathbf{B}_x^{-1} (\mathbf{x}_b - \mathbf{x}) + (\boldsymbol{\beta}_b - \boldsymbol{\beta})^T \mathbf{B}_\beta^{-1} (\boldsymbol{\beta}_b - \boldsymbol{\beta}) + [\mathbf{y} - \mathbf{b}(\mathbf{x}, \boldsymbol{\beta}) - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathbf{b}(\mathbf{x}, \boldsymbol{\beta}) - \mathbf{h}(\mathbf{x})]$$

It works well (even if the model is biased) when the analysis is strongly constrained by observations:



It does not work as well when there are large model biases and observation biases are poorly constrained (e.g., few anchoring observations; many bias-corrected observations with similar characteristics):

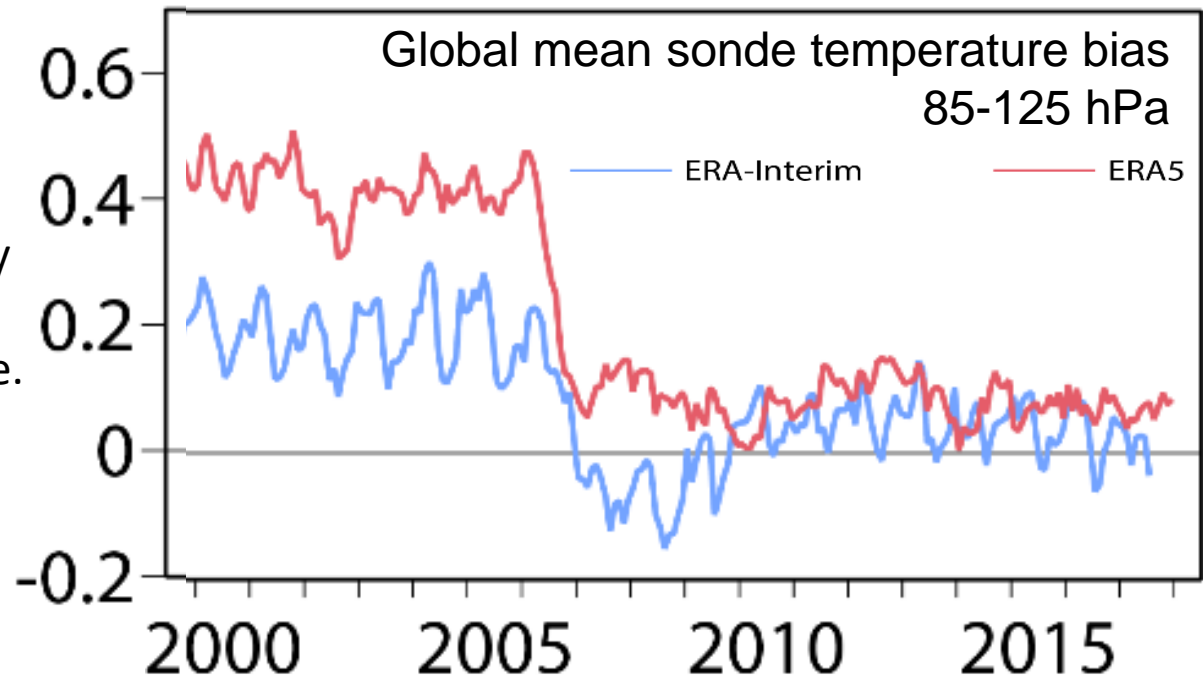
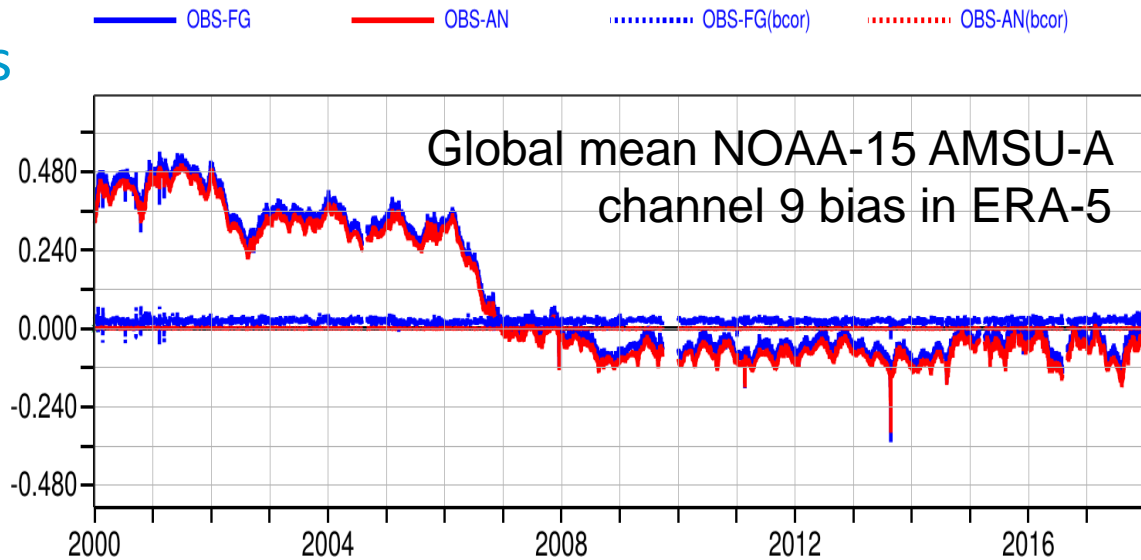


VarBC is not designed to correct model biases: Need for a **weak-constraint 4D-Var (Laloyaux)**

Interaction with model bias and the role of anchor observations

Example: Stratospheric temperature biases

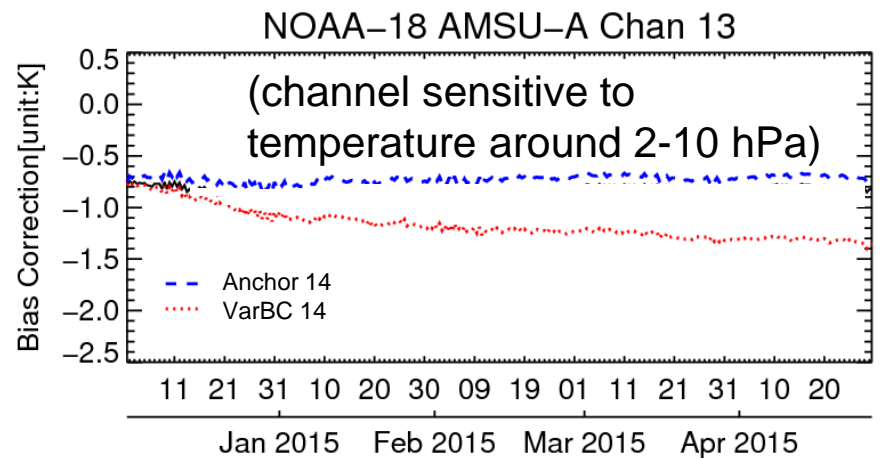
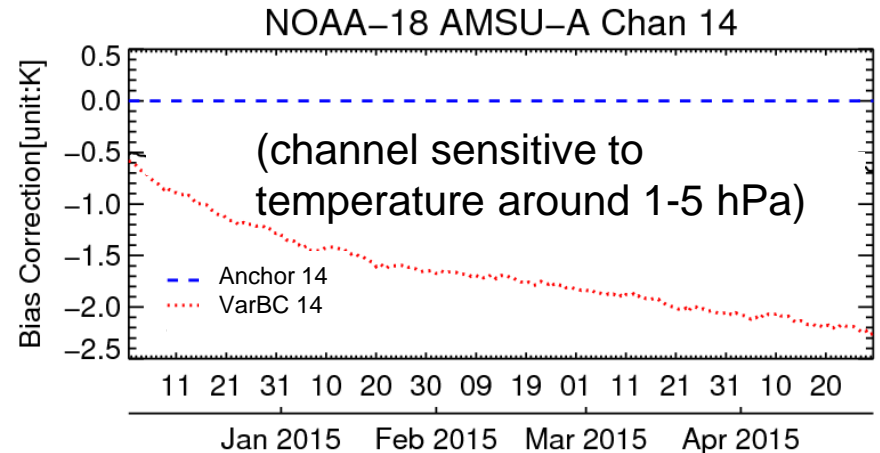
- Model biases affect the bias correction in the absence of sufficient anchor observations.
- GPS-RO provides a good anchor from mid-2006.
- The solution of the bias correction is also affected by other aspects, including the background error covariance.



Interaction with model bias: selecting an anchor

Example: Upper stratospheric temperature biases

- Unrealistic drift in the bias corrections due to model bias (red line)
- Additional *anchoring* can be imposed through assimilating AMSU-A channel 14 without a bias correction (blue line)
- Other anchoring in the ECMWF system: selected ozone-sensitive IR channels



Interaction with model bias: alternative to anchor observations

- Alternative concept to reduce that VarBC corrects model bias:
- **Constrained VarBC** (Han and Bormann 2016):
 - Penalise large bias corrections through an additional term in the cost function.

$$J(\mathbf{x}, \boldsymbol{\beta}) = \frac{1}{2} (\mathbf{x}_b - \mathbf{x})^T \mathbf{B}_x^{-1} (\mathbf{x}_b - \mathbf{x}) + \frac{1}{2} (\boldsymbol{\beta} - \boldsymbol{\beta}_b)^T \mathbf{B}_\beta^{-1} (\boldsymbol{\beta} - \boldsymbol{\beta}_b) + \frac{1}{2} [\mathbf{y} - H(\mathbf{x}) - b(\mathbf{x}, \boldsymbol{\beta})]^T \mathbf{R}^{-1} [\mathbf{y} - H(\mathbf{x}) - b(\mathbf{x}, \boldsymbol{\beta})] + \frac{1}{2} [b(\mathbf{x}, \boldsymbol{\beta}) - \mathbf{b}_0]^T \mathbf{R}_b^{-1} [b(\mathbf{x}, \boldsymbol{\beta}) - \mathbf{b}_0]$$

\mathbf{b}_0 : Priors estimate of observation bias

\mathbf{R}_b : Priors estimate (or on orbit estimation) of radiometric uncertainty

$\boldsymbol{\beta}_b$: Background predictor coefficients

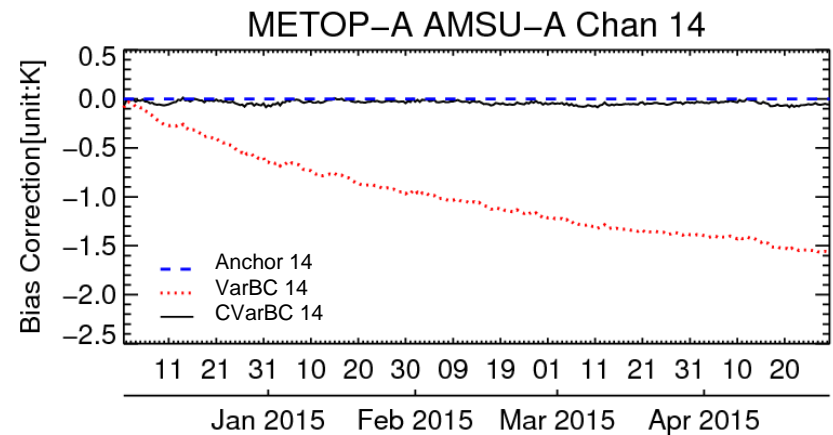
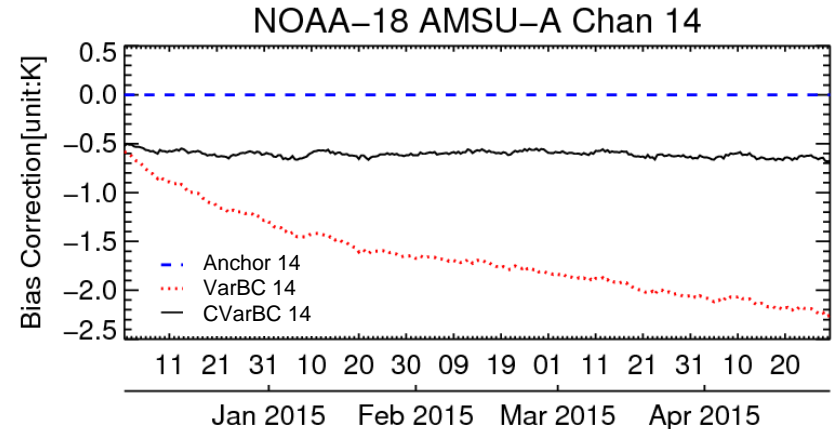
\mathbf{B}_β : Background predictor coefficients uncertainty

Adaptive

Interaction with model bias: alternative constraints

Example: Upper stratospheric temperature biases

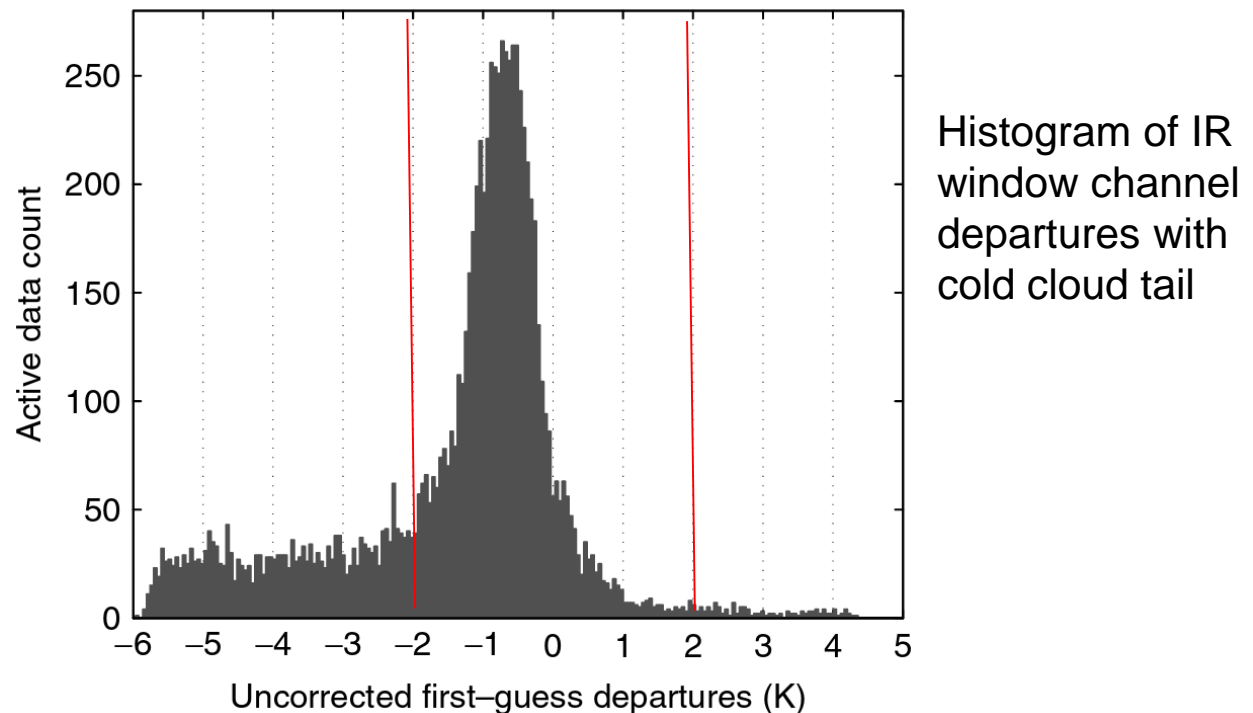
- Constrained VarBC is now used operationally for AMSU-A ch 14 and ATMS ch 15
 - Different bias characteristics for different satellites are now corrected. They were previously ignored when these channels were assimilated without bias correction.
- Further constraints could be introduced by using a more restrictive bias model (e.g., no air-mass component in bias model)



Limitations of VarBC:

Other pit-falls: Removing the signal

- Avoid bias correction models with too many predictors, to avoid correcting for situation-dependent background errors/biases to be incorrectly removed.
- Beware of interaction between VarBC and departure-based quality control and asymmetric distributions:
 - Can lead to unwanted drifts in the population after QC



Summary

Biases are everywhere:

- Most observations cannot be usefully assimilated without bias adjustments
- Manual estimation of biases in satellite data is practically impossible
- Bias estimates can be updated automatically during data assimilation
- Variational bias correction works best in situations where:
 - there is sufficient redundancy in the data; or
 - there are no large model biases

Challenges:

- How to develop good bias models for observations
- How to separate observation bias from model bias

Additional information

- Harris and Kelly, 2001: **A satellite radiance-bias correction scheme for data assimilation.** *Q. J. R. Meteorol. Soc.*, 127, 1453-1468
- Derber and Wu, 1998: **The use of TOVS cloud-cleared radiances in the NCEP SSI analysis system.** *Mon. Wea. Rev.*, 126, 2287-2299
- Dee, 2004: **Variational bias correction of radiance data in the ECMWF system.** Pp. 97-112 in *Proceedings of the ECMWF workshop on assimilation of high spectral resolution sounders in NWP, 28 June-1 July 2004, Reading, UK*
- Dee, 2005: **Bias and data assimilation.** *Q. J. R. Meteorol. Soc.*, 131, 3323-3343
- Dee and Uppala, 2009: **Variational bias correction of satellite radiance data in the ERA-Interim reanalysis.** *Q. J. R. Meteorol. Soc.*, 135, 1830-1841
- Han and Bormann, 2016: **Constrained adaptive bias correction for satellite radiance assimilation in the ECMWF 4D-Var system.** *ECMWF Technical Memorandum 783.*

Feel free to contact me with questions:

Niels.Bormann@ecmwf.int

